

# **Discrete Mathematics**

## Computational Thinking

1. Formulate the Question in English.
2. Determine the Problem you need to Solve.
3. List all the pertinent Parameters.
4. Build a Mathematical Model -- Formulas, Equations, . . .
5. Construct an Algorithm to Solve the Problem.
6. Develop Data Structures and Code to Implement Algorithm.

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### 4. *Build a Mathematical Model*

- Standard Mathematical Methods?

### 5. *Construct an Algorithm*

- Standard Algorithms?
- Proofs of Correctness?

### 6. *Develop Data Structures*

- Standard Data Structures?

## **Mathematical Tools of the Trade**

### *Mathematical Methods*

- Combinatorics and Probability
- Functions, Sets, Relations, . . .

### *Proof Techniques*

- Induction and Logic

### *Algorithms*

- Shortest Path Algorithms
- Searching and Sorting Algorithms

### *Theorems*

- Binomial Theorem

### *Data Structures*

- Graphs and Trees

## Discrete Math vs. Continuous Math

Discrete

Continuous

**N** or **Z**

**R** or **C**

Counting

Limiting

Sequences (Discrete Functions)

Continuous Functions

Sums

Integrals

Differences

Derivatives

## Discrete Math vs. Continuous Math (continued)

Discrete

Continuous

Number Theory\*

Calculus

Digital

Analog

\* Other Topics -- logic, proofs, recursion, induction, combinatorics, probability, sets, functions, relations, regular languages, finite automata,...

## Why Discrete Mathematics in Computer Science

- Digital Computers
- Discrete Data Structure
  - Lists, Trees, Graphs, Sets, ...
- Discrete Programs
- Mathematical Tools of the Trade
  - Not just Programming Languages
  - Data Structures
  - Mathematical Methods -- logic, recursion, relations, combinatorics, probability
  - Algorithms and their Correctness



# **Motivation for Discrete Mathematics**

*Many, Many Applications*

*Fundamental Data Structures*

*Neat Algorithms*

*Engaging Theory*

*Novel Mathematics*