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# Message Passing and MPI

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# Topics

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- **Principles of message passing**
  - building blocks (send, receive)
- **MPI: Message Passing Interface**
- **Overlapping communication with computation**
- **Topologies**
- **Collective communication and computation**
- **Groups and communicators**
- **MPI derived data types**
- **Threading**
- **Remote Memory Access (RMA)**
- **Using MPI**
- **MPI Resources**

# Message Passing Overview

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- The logical view of a message-passing platform
  - $p$  processes
  - each with its own exclusive address space
- All data must be explicitly partitioned and placed
- All interactions (read-only or read/write) are two-sided
  - process that has the data sends it
  - process that wants the data receives it
- Typically use single program multiple data (SPMD) model
- The bottom line ...
  - strengths
    - simple performance model: underlying costs are explicit
    - portable high performance
  - weakness: two-sided model can be awkward to program

# Pros and Cons of Message Passing

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- **Advantages**

- universality

- works well on machines with fast or slow network

- expressivity

- useful and complete model for expressing parallel algorithms

- lack of data races

- data races are a pervasive problem for shared memory programs\*

- performance

- yields high performance by co-locating data with computation

- **Disadvantages**

- managing partitioned address spaces is a hassle

- two-sided communication is somewhat awkward to write

- debugging multiple is awkward

\* MPI is not devoid of race conditions, but they can only occur when non-blocking operations are used

# Message Passing Flavors: Blocking, Unbuffered

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- **Definition**

- send won't return until its data has been transferred
- receive won't return until data has arrived
- no copy is made of the message data

- **Advantage:**

- simple to use

- **Disadvantages**

- send and recv may **idle**, awaiting partner
- deadlock** is possible since send operations block

Processor 0

send x to proc 1

receive y from proc 1

Processor 1

send y to proc 0

receive x from proc 0

# Message Passing Flavors: Blocking, Buffered

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- **Definition**

- send won't return until its data may be overwritten
  - may return after data copied into a buffer at sender
  - data may be delivered early into a buffer at receiver
- receive won't return until the data has arrived

- **Advantages**

- simple to use
- avoids deadlock caused by send

- **Disadvantages**

- receive may **idle**, awaiting a send
- deadlock** still possible since receive operations block

Processor 0

```
receive y from proc 1  
send x to proc 1
```

Processor 1

```
receive x from proc 0  
send y to proc 0
```

# Buffered Blocking Message Passing

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Buffer sizes can have significant impact on performance

## Processor 0

```
for (i = 0; i < N; i++)  
    produce_data(&a)  
    send a to proc 1
```

## Processor 1

```
for (i = 0; i < N; i++)  
    receive a from proc 0  
    consume_data(&a)
```

**Larger buffers enable the computation to tolerate asynchrony better**

# Message Passing Flavors: Non-Blocking

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- **Definition**

- send and receive return before it is safe
  - sender: data can be overwritten before it is sent
  - receiver: can read data out of buffer before it is received
- ensuring proper usage is the programmer's responsibility
- status check operation to ascertain completion

- **Advantages**

- tolerate asynchrony
- no costly copies or buffer space
- overlap communication with computation

- **Disadvantage**

- programming complexity

Processor 0

```
start_send x to proc 1
start_rcv y from proc 1
. . .
end_send x to proc 1
end_rcv y from proc 1
```

Processor 1

```
start_send y to proc 0
start_rcv x from proc 0
. . .
end_send y to proc 0
end_rcv x from proc 0
```

# MPI: the Message Passing Interface

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- **Standard library for message-passing**
  - portable
  - almost ubiquitously available
  - high performance
  - C and Fortran APIs
- **MPI standard defines**
  - syntax of library routines
  - semantics of library routines
- **Details**
  - MPI routines, data-types, and constants are prefixed by “MPI\_”
- **Simple to get started**
  - fully-functional programs using only six library routines

# Scope of the MPI Standards

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- **Communication contexts**
- **Datatypes**
- **Point-to-point communication**
- **Collective communication (synchronous, **non-blocking**)**
- **Process groups**
- **Process topologies**
- **Environmental management and inquiry**
- **The Info object**
- **Process creation and management**
- **One-sided communication (refined for MPI-3)**
- **External interfaces**
- **Parallel I/O**
- **Language bindings for Fortran, C and C++**
- **Profiling interface (PMPI)**

**MPI**  
**MPI-2**  
**MPI-3**

# MPI Primitives at a Glance

Comm File Tool  
RMA Type

MPIX_Comm_agree	MPI_Comm_group	MPI_File_read_all	MPI_Group_free	MPI_Lookup_name	MPI_T_cvar_get_info	MPI_Type_match_size
MPIX_Comm_failure_ack	MPI_Comm_idup	MPI_File_read_all_begin	MPI_Group_incl	MPI_Mprobe	MPI_T_cvar_get_num	MPI_Type_set_attr
MPIX_Comm_failure_get_acked	MPI_Comm_join	MPI_File_read_all_end	MPI_Group_intersection	MPI_Mrecv	MPI_T_cvar_handle_alloc	MPI_Type_set_name
MPIX_Comm_revoke	MPI_Comm_rank	MPI_File_read_at	MPI_Group_range_excl	MPI_Neighbor_allgather	MPI_T_cvar_handle_free	MPI_Type_size
MPIX_Comm_shrink	MPI_Comm_remote_group	MPI_File_read_at_all	MPI_Group_range_incl	MPI_Neighbor_allgatherv	MPI_T_cvar_read	MPI_Type_size_x
MPI_Abort	MPI_Comm_remote_size	MPI_File_read_at_all_begin	MPI_Group_rank	MPI_Neighbor_alltoall	MPI_T_cvar_write	MPI_Type_struct
MPI_Accumulate	MPI_Comm_set_attr	MPI_File_read_at_all_end	MPI_Group_size	MPI_Neighbor_alltoallv	MPI_T_enum_get_info	MPI_Type_sub
MPI_Add_error_class	MPI_Comm_set_errhandler	MPI_File_read_ordered	MPI_Group_translate_ranks	MPI_Neighbor_alltoallw	MPI_T_enum_get_item	MPI_Type_vector
MPI_Add_error_code	MPI_Comm_set_info	MPI_File_read_ordered_begin	MPI_Group_union	MPI_Op_commute	MPI_T_finalize	MPI_Unpack
MPI_Add_error_string	MPI_Comm_set_name	MPI_File_read_ordered_end	MPI_Iallgather	MPI_Op_create	MPI_T_init_thread	MPI_Unpack_external
MPI_Address	MPI_Comm_size	MPI_File_read_shared	MPI_Iallgatherv	MPI_Op_free	MPI_T_pvar_get_info	MPI_Unpublish_name
MPI_Allgather	MPI_Comm_spawn	MPI_File_seek	MPI_Iallreduce	MPI_Open_port	MPI_T_pvar_get_num	MPI_Wait
MPI_Allgatherv	MPI_Comm_spawn_multiple	MPI_File_seek_shared	MPI_Ialltoall	MPI_Pack	MPI_T_pvar_handle_alloc	MPI_Waitall
MPI_Alloc_mem	MPI_Comm_split	MPI_File_set_atomicsity	MPI_Ialltoallv	MPI_Pack_external	MPI_T_pvar_handle_free	MPI_Waitany
MPI_Allreduce	MPI_Comm_split_type	MPI_File_set_errhandler	MPI_Ialltoallw	MPI_Pack_external_size	MPI_T_pvar_read	MPI_Waitsome
MPI_Alltoall	MPI_Comm_test_inter	MPI_File_set_info	MPI_Ibarrrier	MPI_Pack_size	MPI_T_pvar_readreset	MPI_Win_allocate
MPI_Alltoallv	MPI_Compare_and_swap	MPI_File_set_size	MPI_Ibcast	MPI_Pcontrol	MPI_T_pvar_reset	MPI_Win_allocate_shared
MPI_Attr_delete	MPI_Dims_create	MPI_File_set_view	MPI_Ibsend	MPI_Iprobe	MPI_T_pvar_session_create	MPI_Win_attach
MPI_Attr_get	MPI_Dist_graph_create	MPI_File_sync	MPI_Iexscan	MPI_Publish_name	MPI_T_pvar_session_free	MPI_Win_call_errhandler
MPI_Attr_put	MPI_Dist_graph_create_adjacent	MPI_File_write	MPI_Igather	MPI_Put	MPI_T_pvar_start	MPI_Win_complete
MPI_Barrier	MPI_Dist_graph_neighbors	MPI_File_write_all	MPI_Igatherv	MPI_Query_thread	MPI_T_pvar_stop	MPI_Win_create
MPI_Bcast	MPI_Dist_graph_neighbors_count	MPI_File_write_all_begin	MPI_Igprobe	MPI_Raccumulate	MPI_T_pvar_write	MPI_Win_create_dynamic
MPI_Bsend	MPI_Errhandler_create	MPI_File_write_all_end	MPI_Ilrecv	MPI_Recv	MPI_Test	MPI_Win_create_errhandler
MPI_Bsend_init	MPI_Errhandler_free	MPI_File_write_at	MPI_Ineighbor_allgather	MPI_Recv_init	MPI_Test_cancelled	MPI_Win_create_keyval
MPI_Buffer_attach	MPI_Errhandler_get	MPI_File_write_at_all	MPI_Ineighbor_allgatherv	MPI_Reduce	MPI_Testall	MPI_Win_delete_attr
MPI_Buffer_detach	MPI_Errhandler_set	MPI_File_write_at_all_begin	MPI_Ineighbor_alltoall	MPI_Reduce_local	MPI_Testany	MPI_Win_detach
MPI_Cancel	MPI_Error_class	MPI_File_write_at_all_end	MPI_Ineighbor_alltoallv	MPI_Reduce_scatter	MPI_Testsome	MPI_Win_fence
MPI_Cart_coords	MPI_Error_string	MPI_File_write_ordered	MPI_Ineighbor_alltoallw	MPI_Reduce_scatter_block	MPI_Topo_test	MPI_Win_flush
MPI_Cart_create	MPI_Exscan	MPI_File_write_ordered_begin	MPI_Info_create	MPI_Register_dataprep	MPI_Type_commit	MPI_Win_flush_all
MPI_Cart_get	MPI_Fetch_and_op	MPI_File_write_ordered_end	MPI_Info_delete	MPI_Request_free	MPI_Type_contiguous	MPI_Win_flush_local
MPI_Cart_map	MPI_File_c2f	MPI_File_write_shared	MPI_Info_dup	MPI_Request_get_status	MPI_Type_create_darray	MPI_Win_flush_local_all
MPI_Cart_rank	MPI_File_call_errhandler	MPI_Finalize	MPI_Info_free	MPI_Rget	MPI_Type_create_hindexed	MPI_Win_free
MPI_Cart_shift	MPI_File_close	MPI_Finalized	MPI_Info_get	MPI_Rget_accumulate	MPI_Type_create_hindexed_block	MPI_Win_free_keyval
MPI_Cart_sub	MPI_File_create_errhandler	MPI_Free_mem	MPI_Info_get_nkeys	MPI_Rput	MPI_Type_create_hvector	MPI_Win_get_attr
MPI_Cartdim_get	MPI_File_delete	MPI_Gather	MPI_Info_get_nthkey	MPI_Rsend	MPI_Type_create_indexed_block	MPI_Win_get_errhandler
MPI_Cartdim_set	MPI_File_f2c	MPI_Gatherv	MPI_Info_get_valuelen	MPI_Rsend_init	MPI_Type_create_keyval	MPI_Win_get_group
MPI_Close_port	MPI_File_get_amode	MPI_Get	MPI_Info_get_valuelen	MPI_Scan	MPI_Type_create_keyval	MPI_Win_get_info
MPI_Comm_accept	MPI_File_get_atomicsity	MPI_Get_accumulate	MPI_Info_set	MPI_Scatter	MPI_Type_create_resized	MPI_Win_get_name
MPI_Comm_call_errhandler	MPI_File_get_byte_offset	MPI_Get_address	MPI_Init	MPI_Scatterv	MPI_Type_create_struct	MPI_Win_get_name
MPI_Comm_compare	MPI_File_get_errhandler	MPI_Get_address	MPI_Init_thread	MPI_Send	MPI_Type_create_subarray	MPI_Win_lock
MPI_Comm_connect	MPI_File_get_position	MPI_Get_count	MPI_Initialized	MPI_Send_init	MPI_Type_delete_attr	MPI_Win_lock_all
MPI_Comm_create	MPI_File_get_position_shared	MPI_Get_elements	MPI_Intercomm_create	MPI_Sendrecv	MPI_Type_dup	MPI_Win_post
MPI_Comm_create_errhandler	MPI_File_get_size	MPI_Get_elements_x	MPI_Intercomm_merge	MPI_Sendrecv_replace	MPI_Type_extent	MPI_Win_set_attr
MPI_Comm_create_group	MPI_File_get_type_extent	MPI_Get_library_version	MPI_Iprobe	MPI_Ssend	MPI_Type_free	MPI_Win_set_errhandler
MPI_Comm_create_keyval	MPI_File_get_view	MPI_Get_processor_name	MPI_Irecv	MPI_Ssend_init	MPI_Type_free_keyval	MPI_Win_set_info
MPI_Comm_delete_attr	MPI_File_iread	MPI_Get_version	MPI_Ireduce	MPI_Start	MPI_Type_get_attr	MPI_Win_set_name
MPI_Comm_disconnect	MPI_File_iread_at	MPI_Graph_create	MPI_Ireduce_scatter	MPI_Startall	MPI_Type_get_contents	MPI_Win_shared_query
MPI_Comm_dup	MPI_File_iread_at_all	MPI_Graph_get	MPI_Ireduce_scatter_block	MPI_Status	MPI_Type_get_envelope	MPI_Win_start
MPI_Comm_dup_with_info	MPI_File_iread_shared	MPI_Graph_map	MPI_Irsend	MPI_Status_set_cancelled	MPI_Type_get_extent	MPI_Win_sync
MPI_Comm_free	MPI_File_iread_shared	MPI_Graph_map	MPI_Is_thread_main	MPI_Status_set_elements	MPI_Type_get_extent_x	MPI_Win_test
MPI_Comm_free_keyval	MPI_File_iread_shared	MPI_Graph_neighbors	MPI_Iscan	MPI_Status_set_elements_x	MPI_Type_get_name	MPI_Win_unlock
MPI_Comm_get_attr	MPI_File_iread_shared	MPI_Graph_neighbors_count	MPI_Iscatter	MPI_T_category_changed	MPI_Type_get_name	MPI_Win_unlock
MPI_Comm_get_errhandler	MPI_File_iread_shared	MPI_Graph_neighbors_count	MPI_Iscatterv	MPI_T_category_get_categories	MPI_Type_get_true_extent	MPI_Win_unlock_all
MPI_Comm_get_info	MPI_File_iread_shared	MPI_Graphdims_get	MPI_Isend	MPI_T_category_get_cvars	MPI_Type_get_true_extent_x	MPI_Win_wait
MPI_Comm_get_name	MPI_File_iread_shared	MPI_Greqest_complete	MPI_Issend	MPI_T_category_get_info	MPI_Type_hindexed	MPI_Wtick
MPI_Comm_get_parent	MPI_File_iread_shared	MPI_Grequest_start	MPI_Issend	MPI_T_category_get_num	MPI_Type_hvector	MPI_Wtime
	MPI_File_iread_shared	MPI_Group_compare	MPI_Keyval_create	MPI_T_category_get_pvars	MPI_Type_indexed	
	MPI_File_iread_shared	MPI_Group_difference	MPI_Keyval_free		MPI_Type_lb	
	MPI_File_iread_shared	MPI_Group_excl				

# MPI: the Message Passing Interface

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## Minimal set of MPI routines

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<code>MPI_Init</code>	<b>initialize MPI</b>
<code>MPI_Finalize</code>	<b>terminate MPI</b>
<code>MPI_Comm_size</code>	<b>determine number of processes in group</b>
<code>MPI_Comm_rank</code>	<b>determine id of calling process in group</b>
<code>MPI_Send</code>	<b>send message</b>
<code>MPI_Recv</code>	<b>receive message</b>

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# Starting and Terminating the MPI Programs

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- `int MPI_Init(int *argc, char ***argv)`
  - initialization: must call this prior to other MPI routines
  - effects
    - strips off and processes any MPI command-line arguments
    - initializes MPI environment
- `int MPI_Finalize()`
  - must call at the end of the computation
  - effect
    - performs various clean-up tasks to terminate MPI environment
- **Return codes**
  - `MPI_SUCCESS`
  - `MPI_ERROR`

# Communicators

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- **MPI\_Comm: communicator = communication domain**
  - group of processes that can communicate with one another
- **Supplied as an argument to all MPI message transfer routines**
- **Process can belong to multiple communication domains**
  - domains may overlap
- **MPI\_COMM\_WORLD: root communicator**
  - includes all the processes

# Communicator Inquiry Functions

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- `int MPI_Comm_size(MPI_Comm comm, int *size)`  
—determine the number of processes
- `int MPI_Comm_rank(MPI_Comm comm, int *rank)`  
—index of the calling process  
— $0 \leq \text{rank} < \text{communicator size}$

# “Hello World” Using MPI

---

```
#include <mpi.h>
#include <stdio.h>

int main(int argc, char *argv[])
{
    int npes, myrank;
    MPI_Init(&argc, &argv);
    MPI_Comm_size(MPI_COMM_WORLD, &npes);
    MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
    printf("From process %d out of %d, Hello World!\n",
           myrank, npes);
    MPI_Finalize();
    return 0;
}
```

# Sending and Receiving Messages

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- `int MPI_Send(void *buf, int count, MPI_Datatype datatype, int dest_pe, int tag, MPI_Comm comm)`
- `int MPI_Recv(void *buf, int count, MPI_Datatype datatype, int source_pe, int tag, MPI_Comm comm, MPI_Status *status)`
- **Message source or destination PE**
  - index of process in the communicator `comm`
  - receiver wildcard: `MPI_ANY_SOURCE`
    - any process in the communicator can be source
- **Message-tag: integer values,  $0 \leq \text{tag} < \text{MPI\_TAG\_UB}$** 
  - receiver tag wildcard: `MPI_ANY_TAG`
    - messages with any tag are accepted
- **Receiver constraint**
  - message size  $\leq$  buffer length specified

# MPI Primitive Data Types

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MPI data type	C data type
MPI_CHAR	signed char
MPI_SHORT	signed short int
MPI_INT	signed int
MPI_LONG	signed long int
MPI_UNSIGNED_CHAR	unsigned char
MPI_UNSIGNED_SHORT	unsigned short int
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long int
MPI_FLOAT	float
MPI_DOUBLE	double
MPI_LONG_DOUBLE	long double
MPI_BYTE	8 bits
MPI_PACKED	packed sequence of bytes

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# Receiver Status Inquiry

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- `Mpi_Status`

- stores information about an `MPI_Recv` operation

- data structure

```
typedef struct MPI_Status {  
    int MPI_SOURCE;  
    int MPI_TAG;  
    int MPI_ERROR;  
};
```

- `int MPI_Get_count(MPI_Status *status, MPI_Datatype datatype, int *count)`

- returns the count of data items received

- not directly accessible from status variable

# Deadlock with MPI\_Send/Recv?

```
int a[10], b[10], myrank;
MPI_Status s1, s2;
...
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
if (myrank == 0) {
    MPI_Send(a, 10, MPI_INT, 1, 1, MPI_COMM_WORLD);
    MPI_Send(b, 10, MPI_INT, 1, 2, MPI_COMM_WORLD);
}
else if (myrank == 1) {
    MPI_Recv(b, 10, MPI_INT, 0, 2, MPI_COMM_WORLD, &s1);
    MPI_Recv(a, 10, MPI_INT, 0, 1, MPI_COMM_WORLD, &s2);
}
...
```

The diagram illustrates the MPI\_Send and MPI\_Recv calls in the code. A blue oval highlights the destination (1) in both MPI\_Send calls and the destination (0) in both MPI\_Recv calls. A red oval highlights the tag (1) in the first MPI\_Send call and the tag (2) in the second MPI\_Send call, and the tag (2) in the first MPI\_Recv call and the tag (1) in the second MPI\_Recv call. Labels 'destination' and 'tag' with lines pointing to the respective values are shown to the right of the code.

Definition of MPI\_Send says: “This routine **may** block until the message is received by the destination process”

**Deadlock if MPI\_Send is blocking**

# Another Deadlock Pitfall?

---

Send data to neighbor to your right on a ring ...

```
int a[10], b[10], npes, myrank;
MPI_Status status;
...
MPI_Comm_size(MPI_COMM_WORLD, &npes);

MPI_Comm_rank(MPI_COMM_WORLD, &myrank);

MPI_Send(a, 10, MPI_INT, (myrank+1)%npes, 1,
MPI_COMM_WORLD);

MPI_Recv(b, 10, MPI_INT, (myrank-1+npes)%npes, 1,
        MPI_COMM_WORLD, &status);
...
```

**Deadlock if MPI\_Send is blocking**

# Avoiding Deadlock with Blocking Sends

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Send data to neighbor to your right on a ring ...

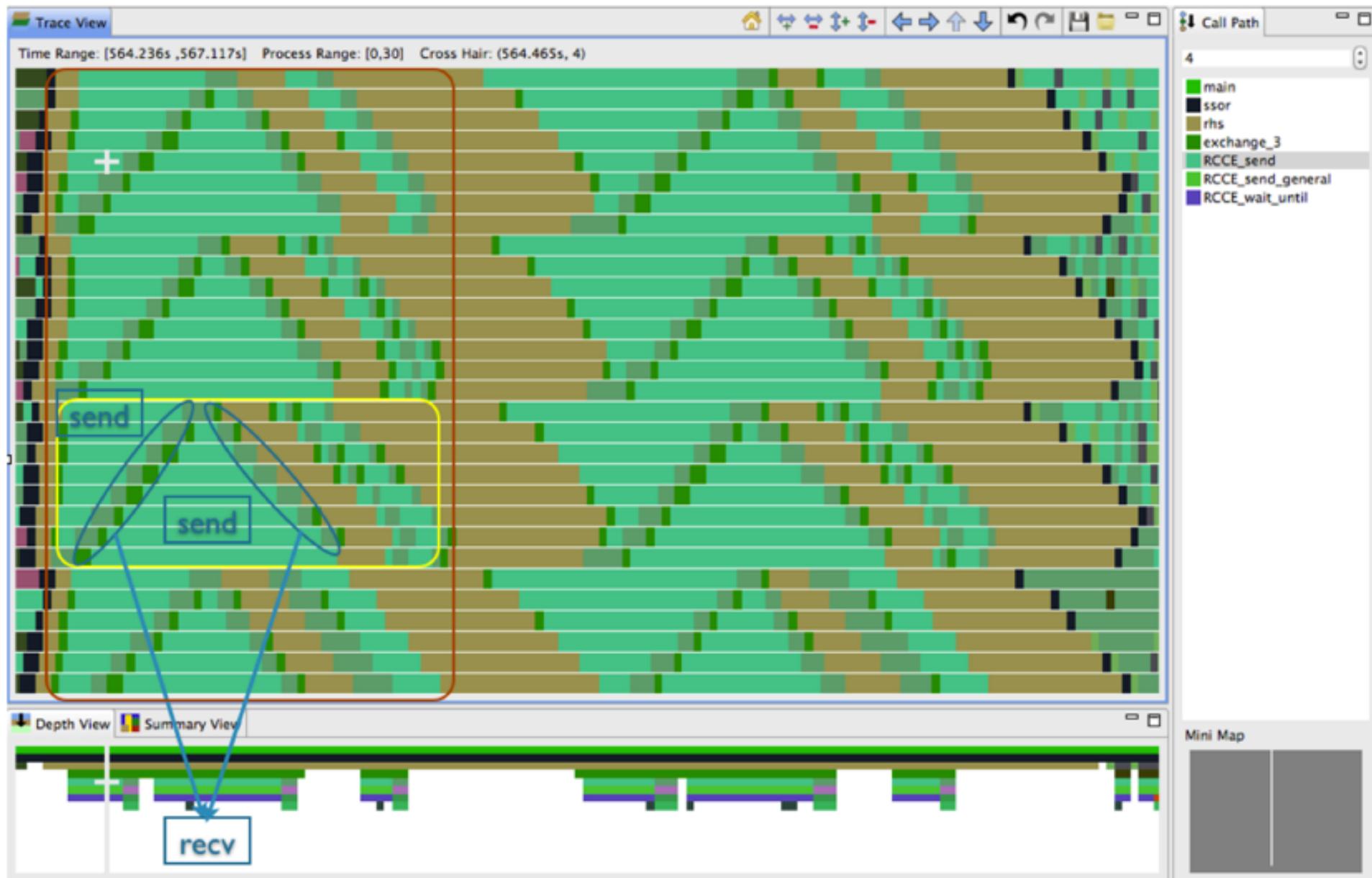
**Break the circular wait**

```
int a[10], b[10], npes, myrank;
MPI_Status status;
...
MPI_Comm_size(MPI_COMM_WORLD, &npes);
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);

if (myrank%2 == 1) { // odd processes send first, receive second
    MPI_Send(a, 10, MPI_INT, (myrank+1)%npes, 1,
             MPI_COMM_WORLD);
    MPI_Recv(b, 10, MPI_INT, (myrank-1+npes)%npes, 1,
             MPI_COMM_WORLD, &status);
}
else { // even processes receive first, send second
    MPI_Recv(b, 10, MPI_INT, (myrank-1+npes)%npes, 1,
             MPI_COMM_WORLD, &status);
    MPI_Send(a, 10, MPI_INT, (myrank+1)%npes, 1,
             MPI_COMM_WORLD);
}
...

```

# Serialization in NAS LU on Intel SCC



# Primitives for Non-blocking Communication

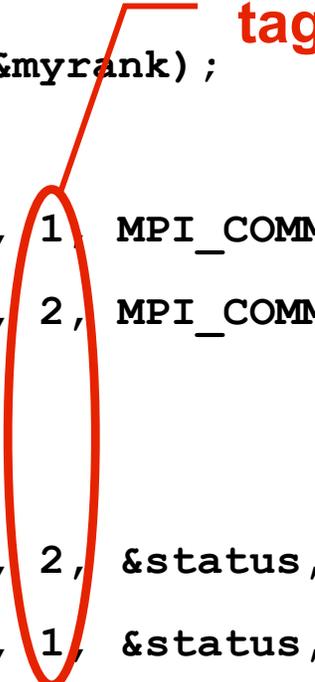
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- **Non-blocking send and receive return before they complete**  
`int MPI_Isend(void *buf, int count, MPI_Datatype datatype,  
int dest, int tag, MPI_Comm comm,  
MPI_Request *request)`  
`int MPI_Irecv(void *buf, int count, MPI_Datatype datatype,  
int source, int tag, MPI_Comm comm,  
MPI_Request *request)`
- **MPI\_Test: has a particular non-blocking request finished?**  
`int MPI_Test(MPI_Request *request, int *flag,  
MPI_Status *status)`
- **MPI\_Waitany: block until some request in a set completes**  
`int MPI_Wait_any(int req_cnt, MPI_Request *req_array,  
int *req_index, MPI_Status *status)`
- **MPI\_Wait: block until a particular request completes**  
`int MPI_Wait(MPI_Request *request, MPI_Status *status)`

# Avoiding Deadlocks with NB Primitives

Using non-blocking operations avoids most deadlocks

```
int a[10], b[10], myrank;
MPI_Request r1, r2;
...
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
if (myrank == 0) {
    MPI_Isend(a, 10, MPI_INT, 1, 1, MPI_COMM_WORLD, &r1);
    MPI_Isend(b, 10, MPI_INT, 1, 2, MPI_COMM_WORLD, &r2);
}
else if (myrank == 1) {
    MPI_Irecv(b, 10, MPI_INT, 0, 2, &status, MPI_COMM_WORLD, &r1);
    MPI_Irecv(a, 10, MPI_INT, 0, 1, &status, MPI_COMM_WORLD, &r2);
}
...
```



# Overlapping Communication Example

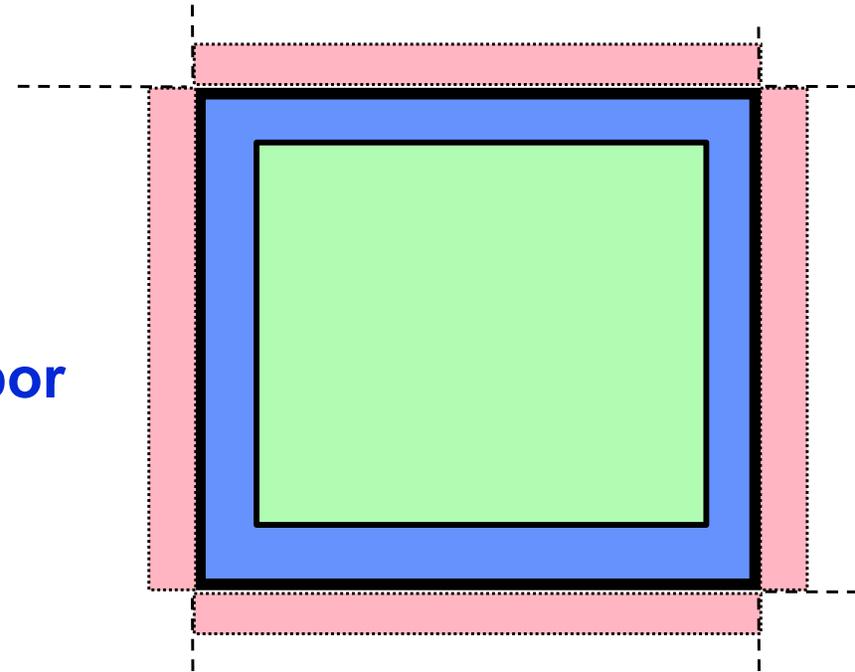
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- **Simple**

- send boundary layer (blue) to neighbors with blocking send
- receive boundary layer (pink) from neighbors
- compute data volume (green + blue)

- **Overlapped**

- send boundary layer (blue) to neighbor with non-blocking send
- compute interior region (green)
- receive boundary layer (pink)
- wait for non-blocking sends to complete (blue)
- compute boundary layer (blue)



# Message Exchange

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**To exchange messages in a single call (both send and receive)**

```
int MPI_Sendrecv(void *sendbuf, int sendcount,  
MPI_Datatype senddatatype, int dest, int sendtag,  
void *recvbuf, int recvcount, MPI_Datatype recvdatatype,  
int source, int recvtag, MPI_Comm comm,  
MPI_Status *status)
```

**Requires both send and receive arguments**

**Why Sendrecv?**

Sendrecv is useful for executing a shift operation along a chain of processes. If blocking send and recv are used for such a shift, then one needs to avoid deadlock with an odd/even scheme. When Sendrecv is used, MPI handles these issues.

**To use same buffer for both send and receive**

```
int MPI_Sendrecv_replace(void *buf, int count,  
MPI_Datatype datatype, int dest, int sendtag,  
int source, int recvtag, MPI_Comm comm,  
MPI_Status *status)
```

# Collective Communication in MPI

---

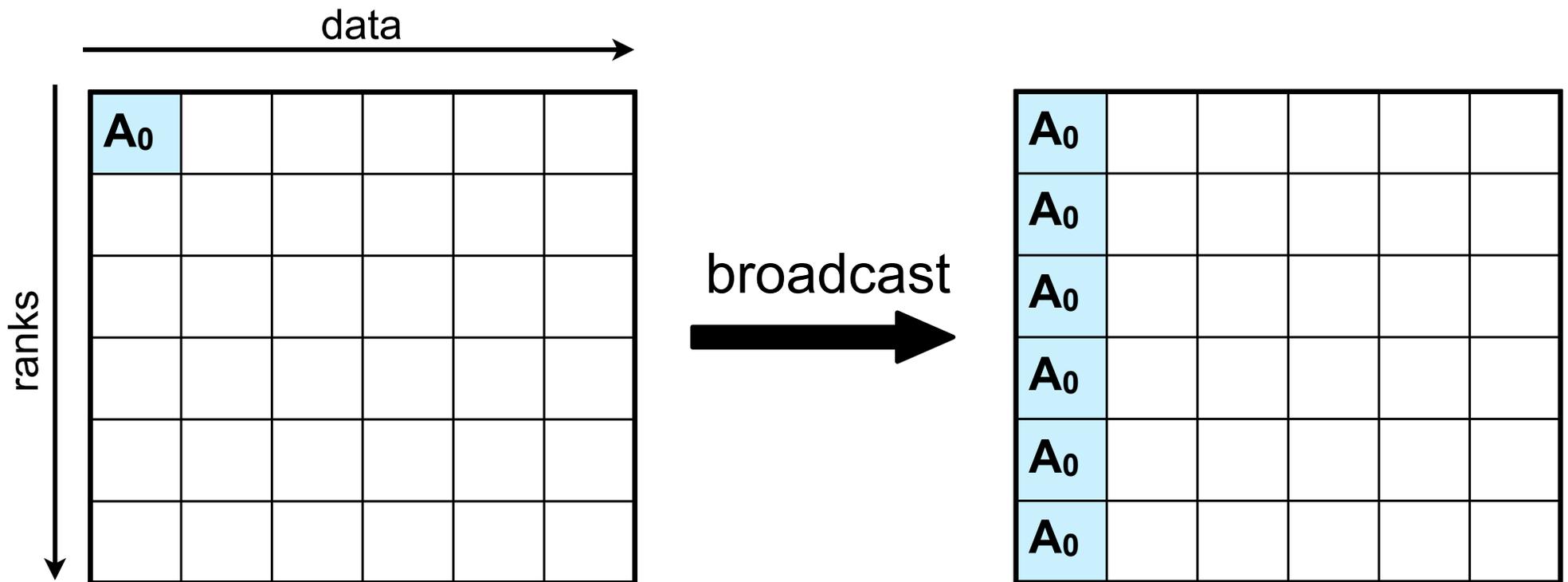
- MPI provides an extensive set of collective operations
- Operations defined over a communicator's processes
- All processes in a communicator must call the same collective operation
  - e.g. all participants in a one-to-all broadcast call the broadcast primitive, even though all but the root are conceptually just “receivers”
- Simplest collective: barrier synchronization

```
int MPI_Barrier(MPI_Comm comm)
```

  - wait until all processes arrive

# One-to-all Broadcast

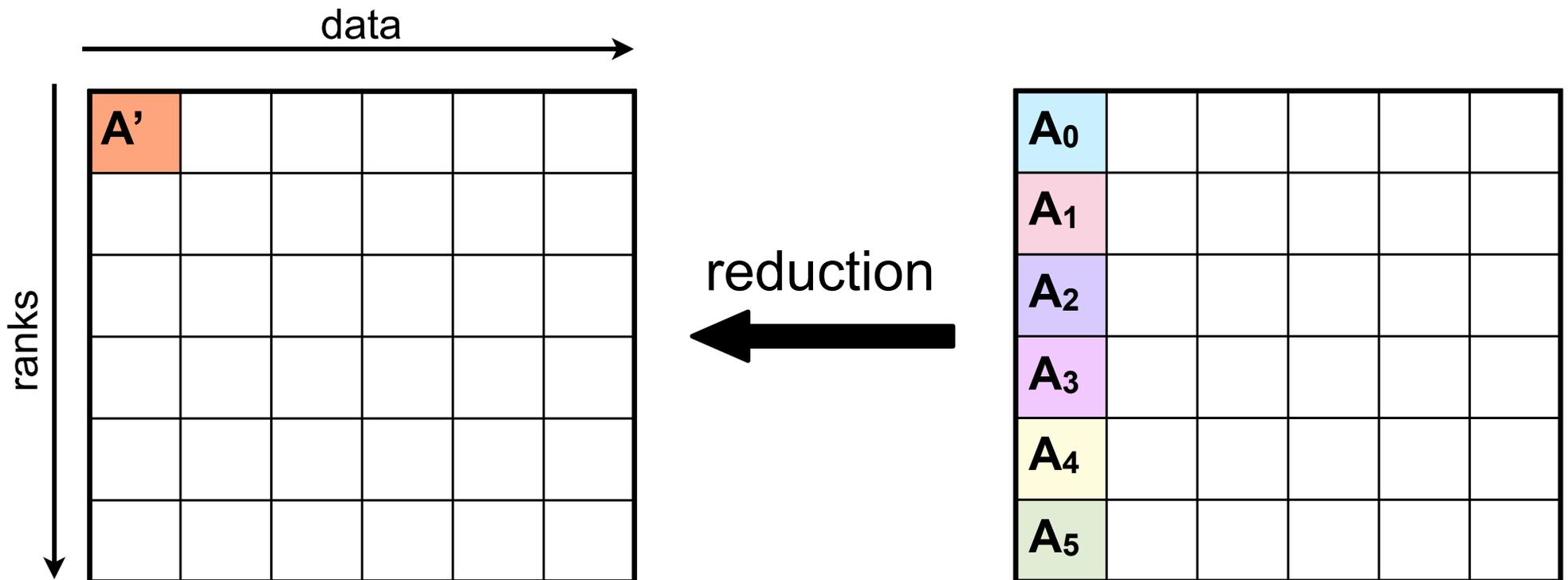
```
int MPI_Bcast(void *buf, int count,  
             MPI_Datatype datatype, int source,  
             MPI_Comm comm)
```



# All-to-one Reduction

```
int MPI_Reduce(void *sendbuf, void *recvbuf,  
              int count, MPI_Datatype datatype,  
              MPI_Op op, int target, MPI_Comm comm)
```

**MPI\_Op examples: sum, product, min, max, ... (see next page)**



$$A' = \text{op}(A_0, A_1, \dots, A_{p-1})$$

# MPI\_Op Predefined Reduction Operations

---

<b>Operation</b>	<b>Meaning</b>	<b>Datatypes</b>
<b>MPI_MAX</b>	<b>Maximum</b>	<b>integers and floating point</b>
<b>MPI_MIN</b>	<b>Minimum</b>	<b>integers and floating point</b>
<b>MPI_SUM</b>	<b>Sum</b>	<b>integers and floating point</b>
<b>MPI_PROD</b>	<b>Product</b>	<b>integers and floating point</b>
<b>MPI_LAND</b>	<b>Logical AND</b>	<b>integers</b>
<b>MPI_BAND</b>	<b>Bit-wise AND</b>	<b>integers and byte</b>
<b>MPI_LOR</b>	<b>Logical OR</b>	<b>integers</b>
<b>MPI_BOR</b>	<b>Bit-wise OR</b>	<b>integers and byte</b>
<b>MPI_LXOR</b>	<b>Logical XOR</b>	<b>integers</b>
<b>MPI_BXOR</b>	<b>Bit-wise XOR</b>	<b>integers and byte</b>
<b>MPI_MAXLOC</b>	<b>Max value-location</b>	<b>Data-pairs</b>
<b>MPI_MINLOC</b>	<b>Min value-location</b>	<b>Data-pairs</b>

---

# MPI\_MAXLOC and MPI\_MINLOC

- Combine pairs of (value, index)

$$\begin{pmatrix} u \\ i \end{pmatrix} \circ \begin{pmatrix} v \\ j \end{pmatrix} = \begin{pmatrix} w \\ k \end{pmatrix}$$

- MPI\_MAXLOC

$$w = \max(u, v) \quad k = \begin{cases} i & \text{if } u > v \\ \min(i, j) & \text{if } u = v \\ j & \text{if } u < v \end{cases}$$

- MPI\_MINLOC

$$w = \min(u, v) \quad k = \begin{cases} i & \text{if } u < v \\ \min(i, j) & \text{if } u = v \\ j & \text{if } u > v \end{cases}$$

value	9	12	14	27	9	27
index	0	1	2	3	4	5

MAXLOC(value,index) = (27, 3)    MINLOC(value,index) = (9, 0)

# Data Types for MINLOC and MAXLOC Reductions

---

**MPI\_MAXLOC and MPI\_MINLOC reductions  
operate on data pairs**

<b>MPI Datatype</b>	<b>C Datatype</b>
<b>MPI_2INT</b>	<b>pair of ints</b>
<b>MPI_SHORT_INT</b>	<b>short and int</b>
<b>MPI_LONG_INT</b>	<b>long and int</b>
<b>MPI_LONG_DOUBLE_INT</b>	<b>long double and int</b>
<b>MPI_FLOAT_INT</b>	<b>float and int</b>
<b>MPI_DOUBLE_INT</b>	<b>double and int</b>

# All-to-All Reduction and Prefix Scan

---

- **All-to-all reduction** - every process gets a copy of the result

```
int MPI_Allreduce(void *sendbuf, void *recvbuf,  
                 int count, MPI_Datatype datatype,  
                 MPI_Op op, MPI_Comm comm)
```

—semantically equivalent to `MPI_Reduce + MPI_Bcast`

- **Parallel prefix operations**

—inclusive scan: processor *i* result = `op(v0, ... vi)`

```
int MPI_Scan(void *sendbuf, void *recvbuf, int count,  
            MPI_Datatype datatype, MPI_Op op,  
            MPI_Comm comm)
```

—exclusive scan: processor *i* result = `op(v0, ... vi-1)`

```
int MPI_Exscan(void *sendbuf, void *recvbuf, int count,  
              MPI_Datatype datatype, MPI_Op op,  
              MPI_Comm comm)
```

# Parallel Prefix Scan

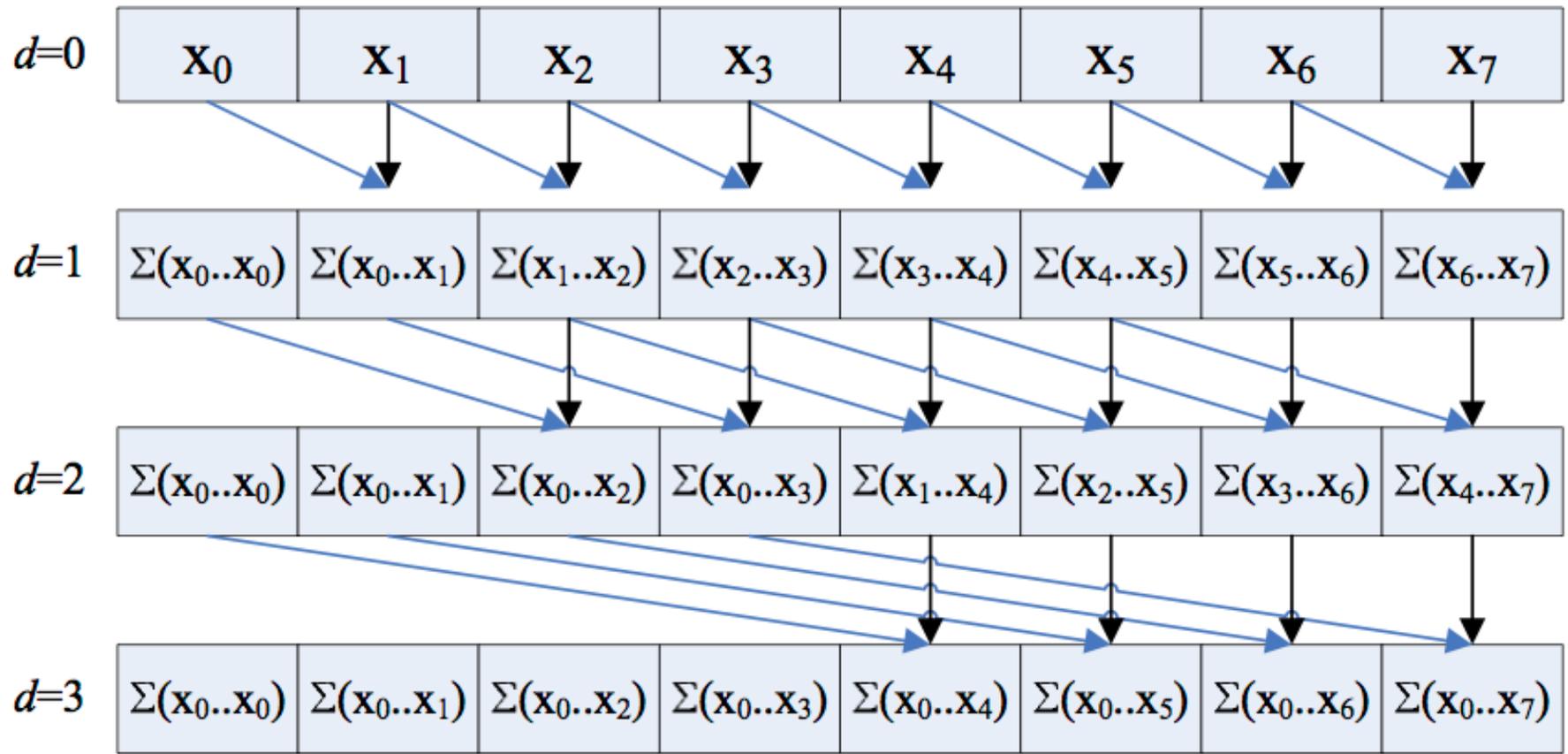
---

- **Inclusive scan:** processor  $i$  result =  $op(v_0, \dots v_i)$
- **Exclusive scan:** processor  $i$  result =  $op(v_0, \dots v_{i-1})$
- **Examples for scans using sum for  $op$**

<b>input</b>	[2	4	1	1	0	1	-3	2	0	6	1	5]
<b>scan</b>	[2	6	7	8	8	9	6	8	8	14	15	20]
<b>exscan</b>	[0	2	6	7	8	8	9	6	8	8	14	15]

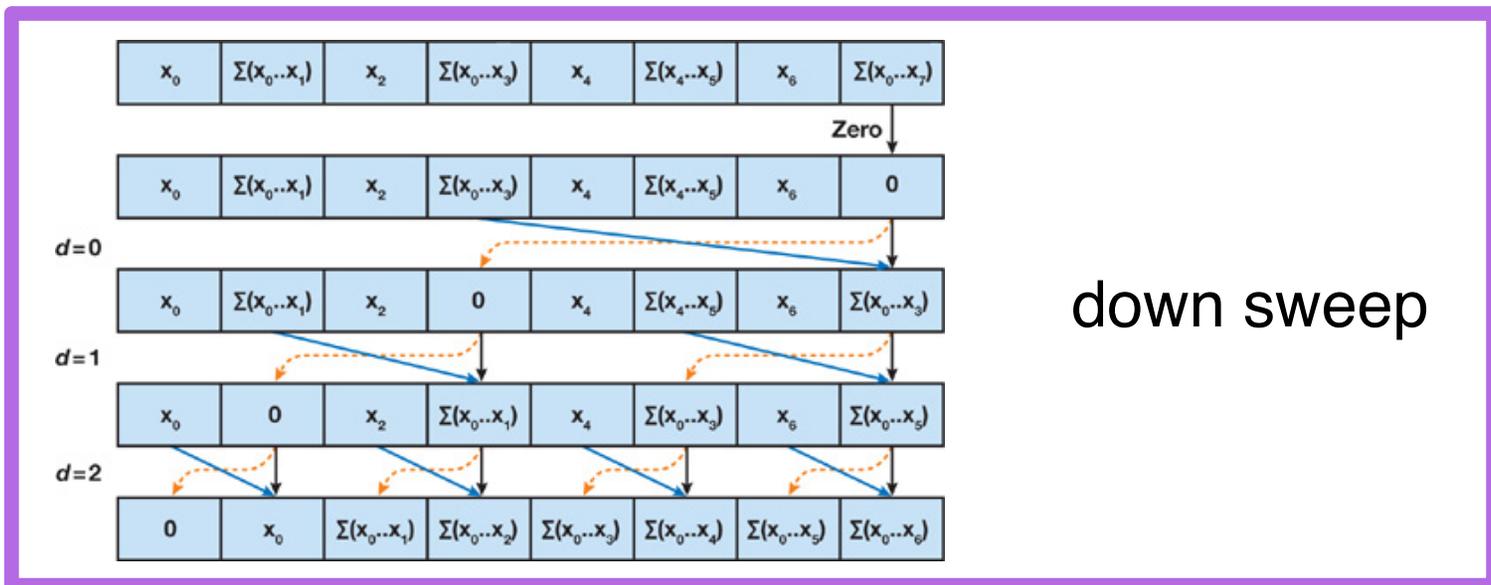
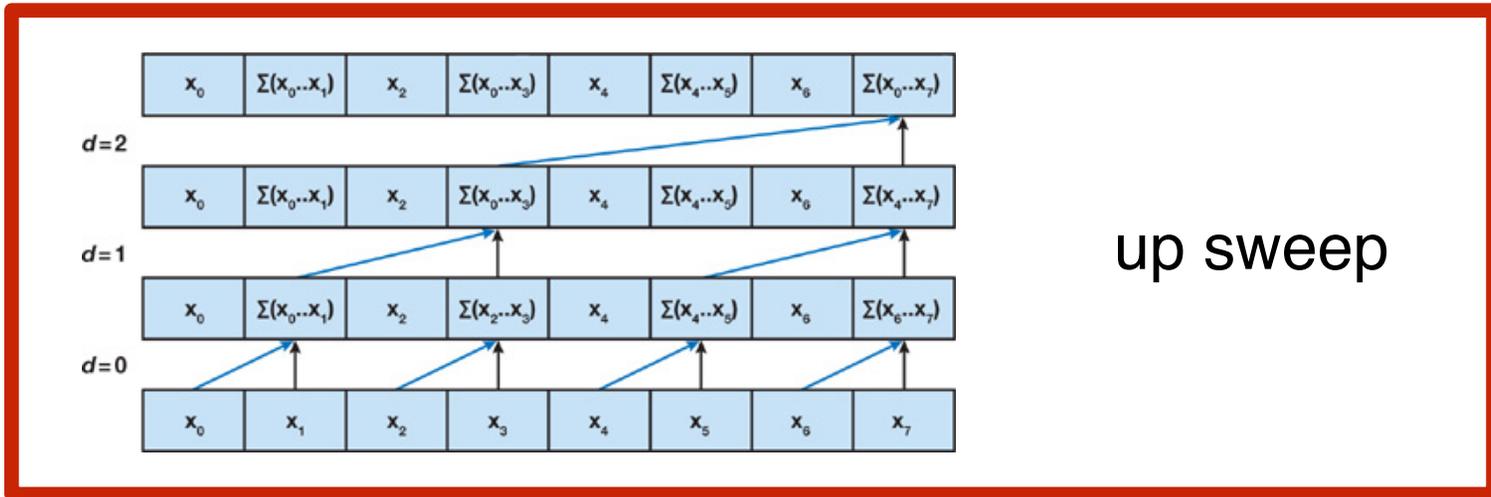
# Inclusive Sum Scan with MPI\_Scan

input     [ 2   4   1   1   0   1  -3   2   0   6   1   5]  
 scan     [ 2   6   7   8   8   9   6   8   8  14  15  20]



# Exclusive Sum Scan with MPI\_Exscan

input	[2	4	1	1	0	1	-3	2	0	6	1	5]
exscan	[0	2	6	7	8	8	9	6	8	8	14	15]



# Scatter/Gather

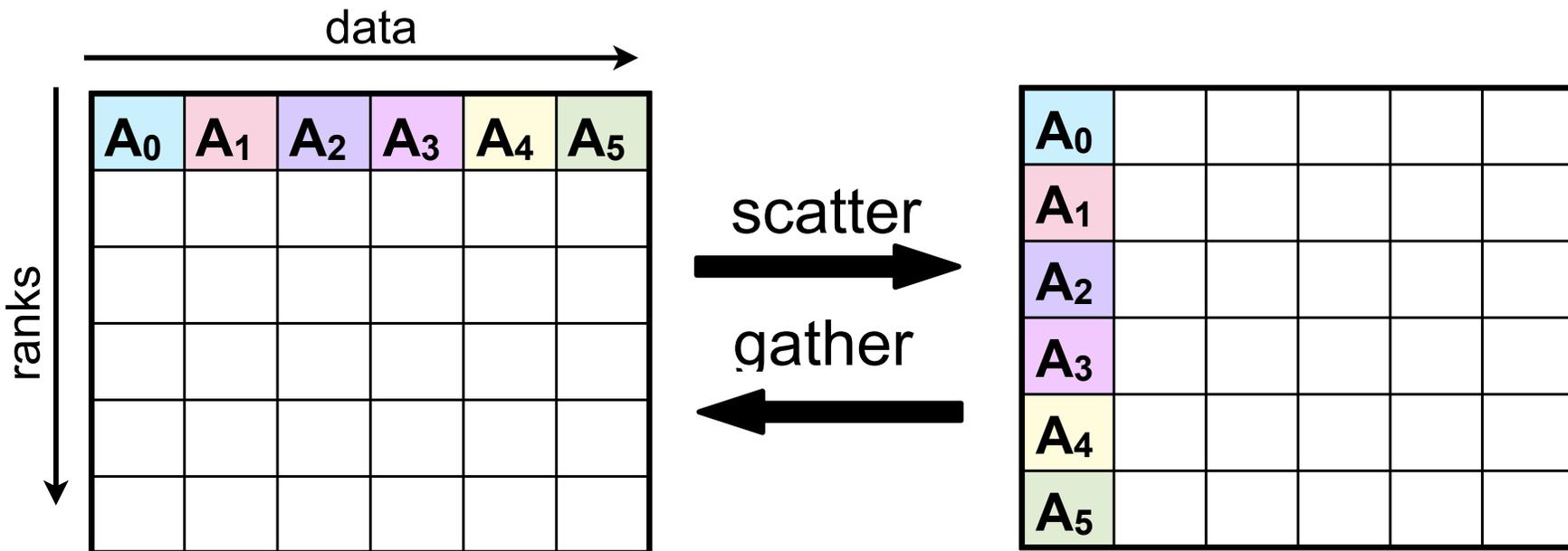
- Scatter data p-1 blocks from root process delivering one to each other

```
int MPI_Scatter(void *sendbuf, int sendcount,  
              MPI_Datatype senddatatype, void *recvbuf,  
              int recvcount, MPI_Datatype recvdatatype,  
              int source, MPI_Comm comm)
```

- Gather data at one process

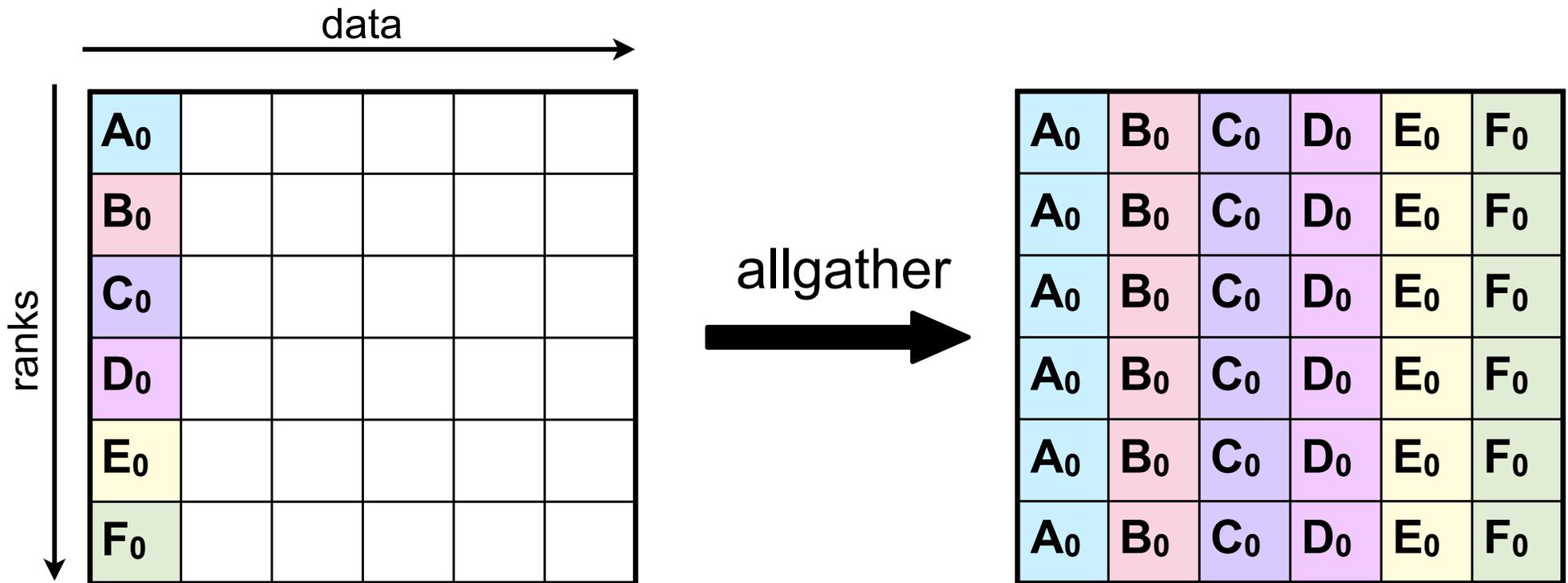
sendcount = number sent to each

```
int MPI_Gather(void *sendbuf, int sendcount,  
              MPI_Datatype senddatatype, void *recvbuf,  
              int recvcount, MPI_Datatype recvdatatype,  
              int target, MPI_Comm comm)
```



# Allgather

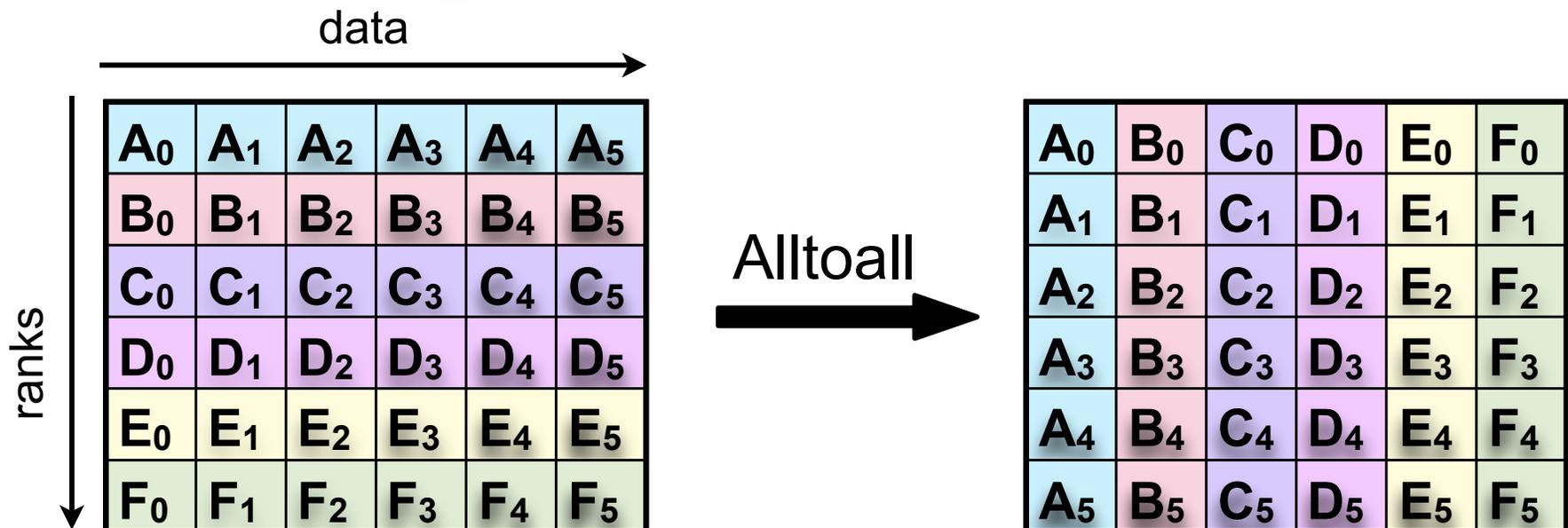
```
int MPI_AllGather(void *sendbuf, int sendcount,  
                 MPI_Datatype senddatatype, void *recvbuf,  
                 int recvcount, MPI_Datatype recvdatatype,  
                 MPI_Comm comm)
```



# All-to-All Personalized Communication

- Each process starts with its own set of blocks, one destined for each process
- Each process finishes with all blocks destined for itself
- Analogous to a matrix transpose

```
int MPI_Alltoall(void *sendbuf, int sendcount,  
                MPI_Datatype senddatatype, void *recvbuf,  
                int recvcount, MPI_Datatype recvdatatype,  
                MPI_Comm comm)
```



# Splitting Communicators

---

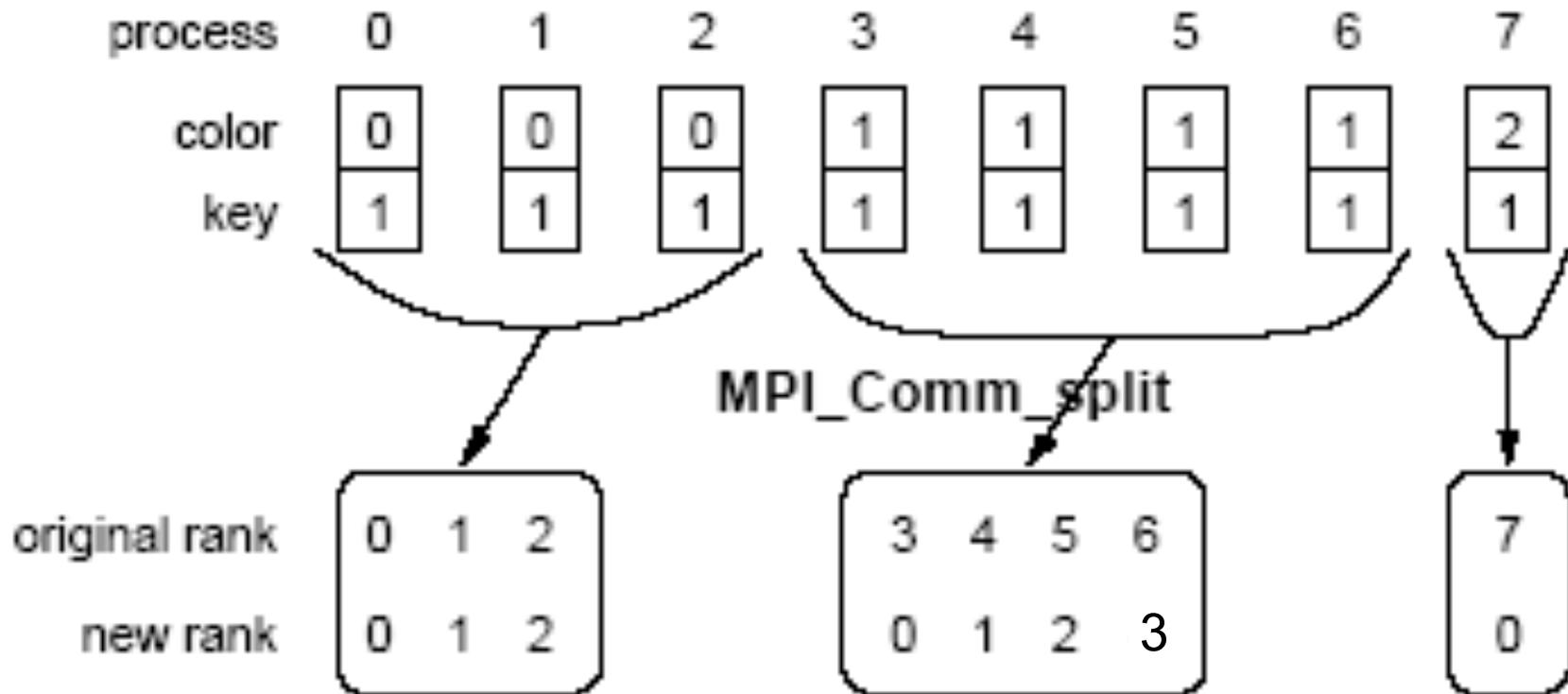
- Useful to partition communication among process subsets
- MPI provides mechanism for partitioning a process group
  - splitting communicators
- Simplest such mechanism

```
int MPI_Comm_split(MPI_Comm comm, int color, int key,  
                  MPI_Comm *newcomm)
```

## —effect

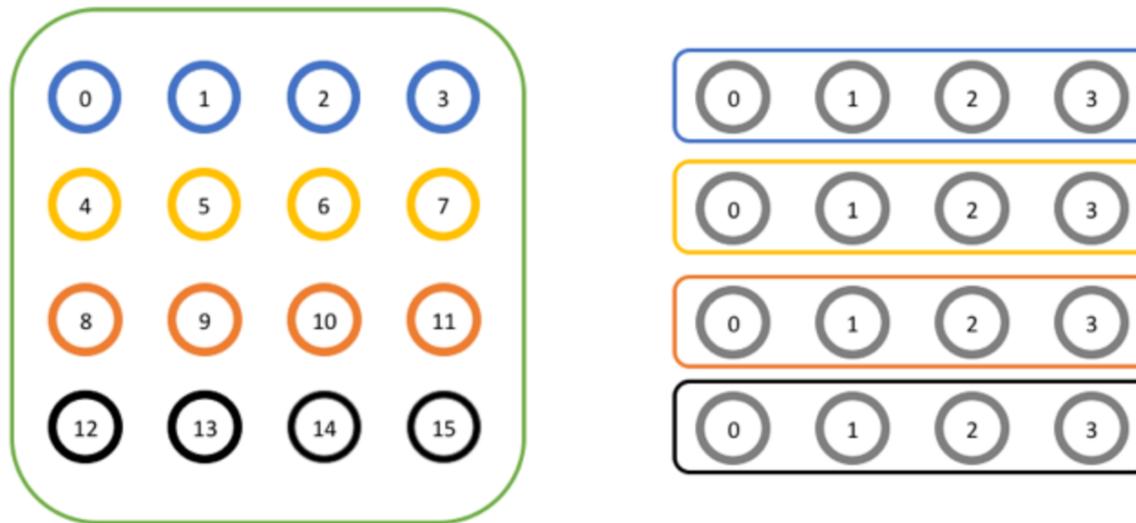
- group processes by color
- sort resulting groups by key

# Splitting Communicators



**Using MPI\_Comm\_split to split a group of processes in a communicator into subgroups**

# Splitting a Communicator



```
// Get the rank and size in the original communicator
int world_rank, world_size;
MPI_Comm_rank(MPI_COMM_WORLD, &world_rank);
MPI_Comm_size(MPI_COMM_WORLD, &world_size);

int color = world_rank / 4; // Determine color based on row

// Split the communicator based on the color and use the
// original rank for ordering
MPI_Comm row_comm;
MPI_Comm_split(MPI_COMM_WORLD, color, world_rank, &row_comm);
```

# Cartesian Topologies

---

- For regular problems a multidimensional mesh organization of processes can be convenient
- Creating a new communicator augmented with a mesh view

```
int MPI_Cart_create(MPI_Comm comm_old, int ndims,  
                   int *dims, int *periods, int reorder,  
                   MPI_Comm *comm_cart)
```

- Map processes into a mesh
  - `ndims` = number of dimensions
  - `dims` = vector with length of each dimension
  - `periods` = vector indicating which dims are periodic
  - `reorder` = flag - ranking may be reordered
- Processor coordinate in cartesian topology
  - a vector of length `ndims`

# Using Cartesian Topologies

---

- **Sending and receiving still requires 1-D ranks**
- **Map Cartesian coordinates  $\Leftrightarrow$  rank**

```
int MPI_Cart_coord(MPI_Comm comm_cart, int rank, int maxdims,  
                  int *coords)
```

```
int MPI_Cart_rank(MPI_Comm comm_cart, int *coords, int *rank)
```

- **Most common operation on cartesian topologies is a shift**
- **Determine the rank of source and destination of a shift**

```
int MPI_Cart_shift(MPI_Comm comm_cart, int dir, int s_step,  
                  int *rank_source, int *rank_dest)
```

# Splitting Cartesian Topologies

---

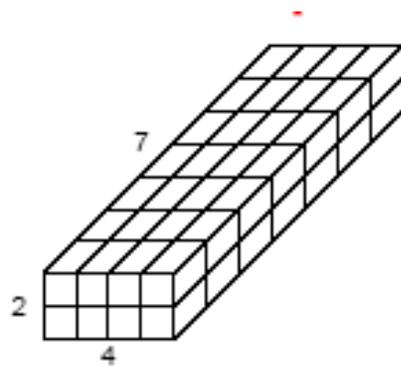
- Processes arranged in a virtual grid using Cartesian topology
- May need to restrict communication to a subset of the grid
- Partition a Cartesian topology to form lower-dimensional grids

```
int MPI_Cart_sub(MPI_Comm comm_cart, int *keep_dims,  
                MPI_Comm *comm_subcart)
```

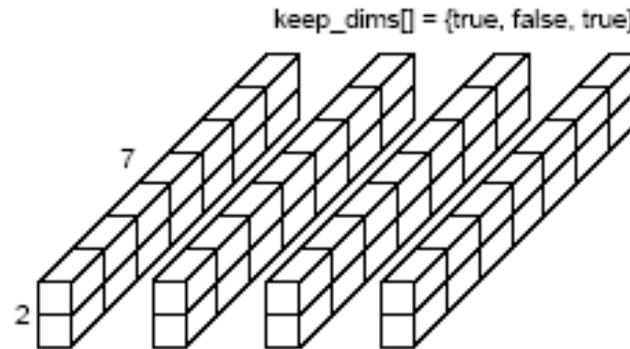
- If `keep_dims[i]` is true (i.e. non-zero in C)
  - `i`<sup>th</sup> dimension is retained in the new sub-topology
- Process coordinates in a sub-topology
  - derived from coordinate in the original topology
  - disregard coordinates for dimensions that were dropped

# Splitting Cartesian Topologies

```
int MPI_Cart_sub(MPI_Comm comm_cart, int *keep_dims,  
                MPI_Comm *comm_subcart)
```

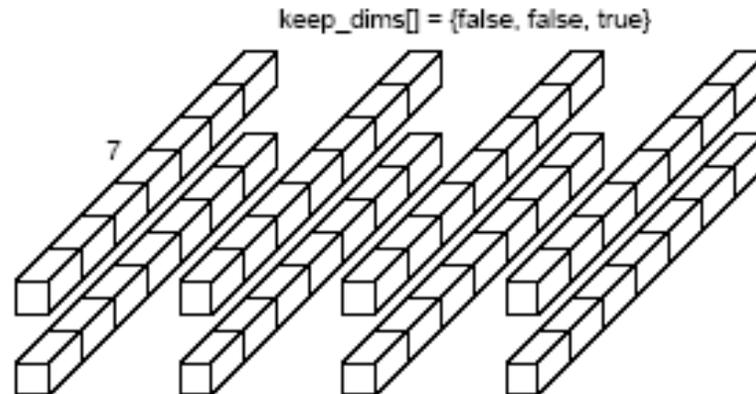


**2 x 4 x 7**



(a)

**4 @ 2 x 1 x 7**



(b)

**8 @ 1 x 1 x 7**

# Graph Topologies

- For irregular problems a graph organization of processes can be convenient

```
int MPI_Graph_create(MPI_Comm comm_old, int nnodes,  
                    int *index, int *edges,  
                    int reorder, MPI_Comm *cgraph)
```

- Map processes into a graph

— `nnodes` = number of nodes

— `index` = vector of integers describing node degrees

— `edges` = vector of integers describing edges

— `reorder` = flag indicating ranking may be reordered

process	neighbors
0	1, 3
1	0
2	3
3	0, 2

```
nnodes = 4  
index = 2, 3, 4, 6  
edges = 1, 3, 0, 3, 0, 2
```

difference between current  
and previous index indicates  
node degree

# Operations on Graph Topologies

---

- Interrogating a graph topology with `MPI_Graphdims_get`

```
int MPI_Graphdims_get(MPI_Comm comm, int *nnodes,  
                      int *nedges)
```

- inquire about length of node and edge vectors

- Extracting a graph topology with `MPI_Graph_get`

```
int MPI_Graph_get(MPI_Comm comm, int maxindex,  
                 int maxedges, int *index,  
                 int *edges)
```

- read out the adjacency list structure in index and edges

# MPI Derived Data Types

---

- A **general datatype** is an opaque object that specifies 2 things
  - a sequence of basic data types
  - a sequence of integer (byte) displacements
    - not required to be positive, distinct, or in increasing order
- Some properties of general data types
  - order of items need not coincide with their order in memory
  - an item may appear more than once
- **Type map** = pair of type & displacement sequences (equivalently, a sequence of pairs)
- **Type signature** = sequence of basic data types

# Building an MPI Data Type

---

```
int MPI_Type_struct(int count, int blocklens[],
    MPI_Aint indices[], MPI_Datatype old_types[],
    MPI_Datatype *newtype )
```

if you define a structure datatype and wish to send or receive multiple items, you should explicitly include an **MPI\_UB** entry as the last member of the structure.

## Example

```
struct { int a; char b; } foo;
```

```
    blen[0]=1; indices[0] = 0;           // offset of a
    oldtypes[0]=MPI_INT;
    blen[1]=1; indices[1] = &foo.b - &foo.a; // offset of b
    oldtypes[1]=MPI_CHAR;
    blen[2]=1; indices[2] = sizeof(foo);   // offset of UB
    oldtypes[2]= MPI_UB;
    MPI_Type_struct( 3, blen, indices, oldtypes, &newtype );
```

# MPI Data Type Constructor Example 1

---

```
int MPI_Type_contiguous(int count, MPI_Datatype oldtype,  
                        MPI_Datatype *newtype)
```

—**newtype** is the datatype obtained by concatenating **count** copies of **oldtype**

- **Example**

—consider constructing **newtype** from the following

- **oldtype** with type map  $\{ ( \textit{double}, 0), ( \textit{char}, 8) \}$ , with extent 16
- let **count** = 3

—type map of **newtype** is

- $\{ ( \textit{double}, 0), ( \textit{char}, 8),$   
 $( \textit{double}, 16), ( \textit{char}, 24),$   
 $( \textit{double}, 32), ( \textit{char}, 40) \}$
- namely, alternating **double** and **char** elements, with displacements **0, 8, 16, 24, 32, 40**

# MPI Data Type Constructor Example 2

---

```
int MPI_Type_vector(int count, int blocklength, int stride,  
                   MPI_Datatype oldtype,  
                   MPI_Datatype *newtype)
```

- Let oldtype have type map  
    { (double, 0), (char, 8) } with extent 16
- A call to MPI\_Type\_vector( 2, 3, 4, oldtype, newtype) will create the datatype with type map  
    —two blocks with three copies each of the old type, with a stride of 4 elements (4 x 16 bytes) between the blocks  
  
    { (double, 0), ( char, 8),     (double, 16), (char, 24),   (double, 32), ( char, 40),  
      (double, 64), (char, 72),   (double, 80), (char, 88),   (double, 96), (char, 104) }

# Threads and MPI

---

- **MPI-2 Specification**
  - does not mandate thread support
  - specifies what a thread-compliant MPI should do
  - specifies four levels of thread support
- **Threads are not addressable**
  - MPI\_Send(... thread\_id ...) is not possible

# Initializing MPI for Threading

---

```
int MPI_Init_thread(int *argc, char ***argv,  
                   int required, int *provided)
```

Used instead of `MPI_Init`; `MPI_Init_thread` has a provision to request a certain level of thread support in **required**

- `MPI_THREAD_SINGLE`: only one thread will execute
- `MPI_THREAD_FUNNELED`: if the process is multithreaded, only the thread that called `MPI_Init_thread` will make MPI calls
- `MPI_THREAD_SERIALIZED`: if the process is multithreaded, only one thread will make MPI library calls at one time
- `MPI_THREAD_MULTIPLE`: if the process is multithreaded, multiple threads may call MPI at once with no restrictions

Require the lowest level that you need

`MPI_Init` is equivalent to supplying `MPI_THREAD_SINGLE` to `MPI_Init_thread`

# Thread-compliant MPI

- All MPI library calls are thread safe
- Blocking calls block the calling thread only  
—other threads can continue executing



# MPI Threading Inquiry Primitives

---

- Inquire about what kind of thread support MPI has provided to your application

```
int MPI_Query_thread(int *provided)
```

- Inquire whether this thread called MPI\_Init or MPI\_Init\_thread

```
int MPI_Is_thread_main(int *flag)
```

# MPI + Threading Example

---

```
#include "mpi.h"
#include <stdio.h>

int main( int argc, char *argv[] )
{
    int errs = 0;
    int provided, flag, claimed;
    pthread_t thread;

    MPI\_Init\_thread( 0, 0, MPI_THREAD_MULTIPLE, &provided );

    MPI\_Is\_thread\_main( &flag );
    if (!flag) {
        errs++;
        printf( "This thread called init_thread but Is_thread_main gave false\n" );
        fflush(stdout);
    }
    MPI\_Query\_thread( &claimed );
    if (claimed != provided) {
        errs++;
        printf( "Query thread gave thread level %d but Init_thread gave %d\n", claimed, provided );
        fflush(stdout);
    }
    pthread_create(&thread, NULL, mythread_function, NULL);
    ...

    MPI\_Finalize();
    return errs;
}
```

# One-Sided vs. Two-Sided Communication

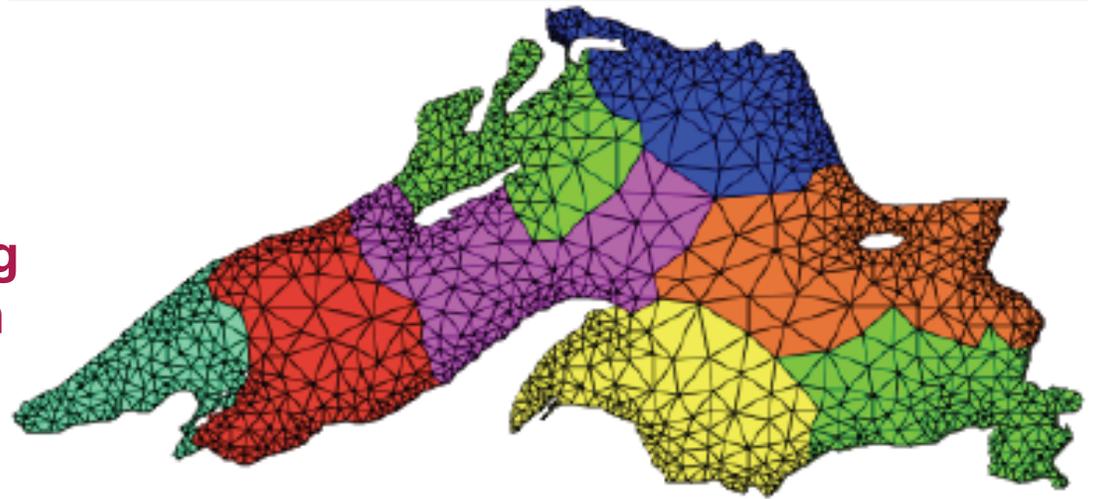
---

- **Two-sided: data transfer and synchronization are conjoined**
  - message passing communication is two-sided
    - sender and receiver issue explicit send or receive operations to engage in a communication
- **One-sided: data transfer and synchronization are separate**
  - a process or thread of control can read or modify remote data without explicit pairing with another process
  - terms
    - origin process: process performing remote memory access
    - target process: process whose data is being accessed

# Why One-Sided Communication?

- If communication pattern is not known a priori, using a two-sided (send/rcv) model requires an extra step to determine how many sends-recvs to issue on each processor

Consider the communication associated with acquiring information about neighboring vertices in a partitioned graph



- Easier to code using one-sided communication because only the origin or target process needs to issue the put or get call
- Expose hardware shared memory
  - more direct mapping of communication onto HW using load/store
    - avoid SW overhead of message passing; let the HW do its thing!

# One-Sided Communication in MPI-2

---

- **MPI-2 Remote Memory Access (RMA)**
  - processes in a communicator can read, write, and accumulate values in a region of “shared” memory
- **Two aspects of RMA-based communication**
  - data transfer, synchronization
- **RMA advantages**
  - multiple data transfers with a single synchronization operation
  - can be significantly faster than send/recv on some platforms
    - e.g. systems with hardware support for shared memory

# MPI-2 RMA Operation Overview

---

- **MPI\_Win\_create**
  - collective operation to create new window object
  - exposes memory to RMA by other processes in a communicator
- **MPI\_Win\_free**
  - deallocates window object
- **Non-blocking data movement operations**
  - MPI\_Put**
    - moves data from local memory to remote memory
  - MPI\_Get**
    - retrieves data from remote memory into local memory
  - MPI\_Accumulate**
    - updates remote memory using local values
- **Synchronization operations**

# Active Target vs. Passive Target RMA

---

- **Passive target RMA**
  - target process makes no synchronization call
- **Active target RMA**
  - requires participation from the target process in the form of synchronization calls (fence or post/wait, start/complete)
- **Illegal to have overlapping active and passive RMA epochs**

# Synchronization for Passive Target RMA

---

- **MPI\_Win\_lock(locktype, target\_rank, assert, win)** “beginning RMA”
  - locktype values**
    - **MPI\_LOCK\_EXCLUSIVE**
      - one process at a time may access
      - use when modifying the window
    - **MPI\_LOCK\_SHARED**
      - multiple processes
        - (as long as none hold MPI\_LOCK\_EXCLUSIVE)
        - useful when accessing window only with MPI\_Get
  - assert values**
    - **0**
    - **MPI\_MODE\_NOCHECK**
- **MPI\_Win\_unlock(target\_rank, win)** “ending RMA”

# Active Target Synchronization

- **MPI\_Win\_start**
  - begins an RMA epoch on origin process
- **MPI\_Win\_post**
  - starts RMA exposure for a local window on a target process
- **MPI\_Win\_wait/test**
  - end RMA exposure on local window on a target process
- **MPI\_Win\_complete**
  - forces local completion an RMA epoch on origin
- **MPI\_Win\_fence**
  - collective forces remote completion of put/get/acc before fence

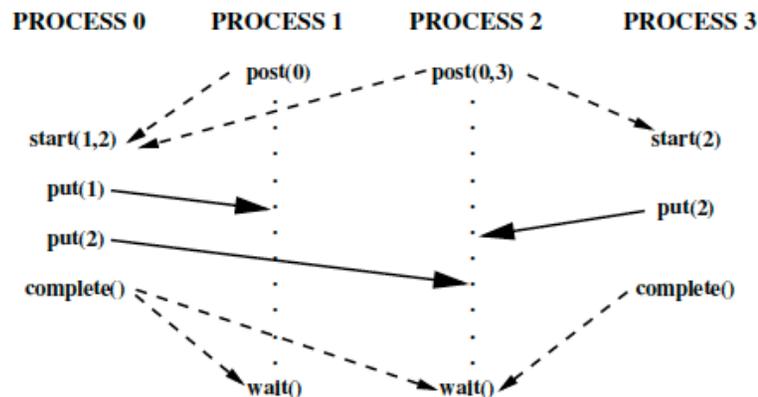


Figure credit:  
MPI-3 draft  
specification,  
Nov. 2010.

# MPI RMA Active Target Example 1

---

**Generic loosely synchronous, iterative code, using fence synchronization**

The window at each process consists of array A, which contains the origin and target buffers of the Get calls

```
...
while (!converged(A)) {
    update_boundary(A);
    MPI_Win_fence(MPI_MODE_NOPRECEDE, win);
    for(i=0; i < toneighbors; i++)
        MPI_Get(&tobuf[i], 1, totype[i], fromneighbor[i],
                fromdisp[i], 1, fromtype[i], win);
    update_core(A);
    MPI_Win_fence(MPI_MODE_NOSUCCEED, win);
}
```

Similar code could be written with Put rather than Get

# MPI RMA Active Target Example 2

---

**Generic loosely synchronous, iterative code, using fence synchronization**

The window at each process consists of array A, which contains the origin and target buffers of the Get calls

```
...
while (!converged(A)) {
    update_boundary(A);
    MPI_Win_post(togroup, win);
    MPI_Win_start(fromgroup, win);
    for(i=0; i < toneighbors; i++)
        MPI_Get(&tobuf[i], 1, totype[i], fromneighbor[i],
                fromdisp[i], 1, fromtype[i], win);
    update_core(A);
    MPI_Win_complete(win);
}
```

Similar code could be written with Put rather than Get

# MPI-1 Profiling Interface - PMPI

---

- To support tools, MPI implementations define two interfaces to every MPI function
  - MPI\_xxx
  - PMPI\_xxx
- One can “wrap” MPI functions with a tool library to observe execution of an MPI program

```
int MPI_Send(void* buffer, int count, MPI_Datatype dtype,
             int dest, int tag, MPI_Comm comm)
{
    double tstart = MPI_Wtime(); /* Pass on all arguments */
    int extent;
    int result = PMPI_Send(buffer, count, dtype, dest, tag, comm);
    MPI_Type_size(dtype, &extent); /* Compute size */
    totalBytes += count*extent;
    totalTime += MPI_Wtime() - tstart; /* and time */
    return result;
}
```

# Some MPI Tools

- **MPICH MPI implementation**
  - MPI tracing library
  - Jumpshot trace visualization tool
- **Vampir: MPI trace analysis tools**
  - <http://www.vampir.eu/>
- **MPIp library for profiling MPI operations**
  - <http://mpip.sourceforge.net>
- **memcheck**
  - OpenMPI + valgrind checks correct use of comm buffers
  - <http://www.open-mpi.org>
- **marmot**
  - checks usage of MPI routines
  - <http://www.hlr.de/organization/av/amt/projects/marmot>



Vampir displays

# MPI Libraries

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- **SCALAPACK** - dense linear algebra using block-cyclic tilings  
—[http://www.netlib.org/scalapack/scalapack\\_home.html](http://www.netlib.org/scalapack/scalapack_home.html)
- **PetSC** - Portable Extensible, Toolkit for Scientific Computation  
—data structures and routines for solution of scientific applications modeled by partial differential equations  
—<http://www.mcs.anl.gov/petsc/petsc-as>
- **Trilinos** - software framework for solving large-scale, complex multi-physics engineering and scientific problems  
—<http://trilinos.sandia.gov>

# MPI-3 Additions

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## Nonblocking collective operations

- barrier synchronization
- broadcast
- gather
- scatter
- gather-to-all
- all-to-all scatter/gather
- reduce
- reduce-scatter
- inclusive scan
- exclusive scan

# Building MPI Programs

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- **Each MPI installation defines compilation scripts**
  - mpicc: C
  - mpif90: Fortran 90
  - mpif77: Fortran 77
  - mpicxx, mpiCC: C++
- **Benefits of using these scripts**
  - they supply the appropriate paths
    - for MPI include files
    - for MPI library files
  - they link appropriate libraries into your executable

# Common Errors and Misunderstandings

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- **Expecting argc and argv to be passed to all processes**
  - some MPI implementations pass them to all processes, but the MPI standard does not require it
- **Doing things before MPI\_Init or after MPI\_Finalize**
  - the MPI standard says nothing about the state of an execution outside this interval
- **Matching MPI\_Bcast with MPI\_Recv; all should use MPI\_Bcast**
- **Assuming your MPI implementation is thread safe**

# Running MPI Programs

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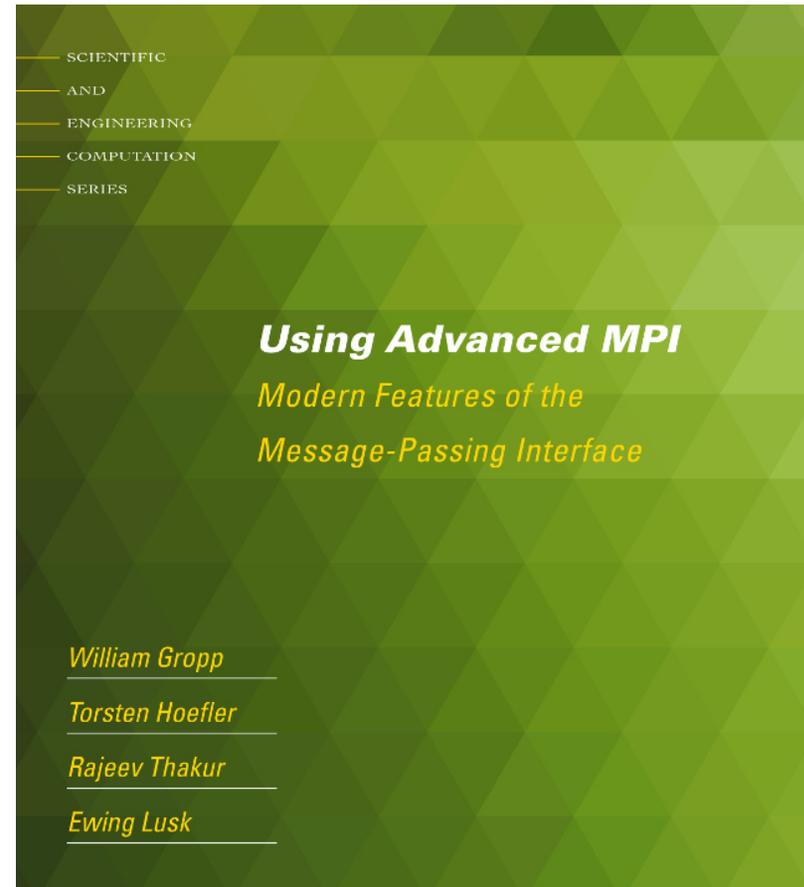
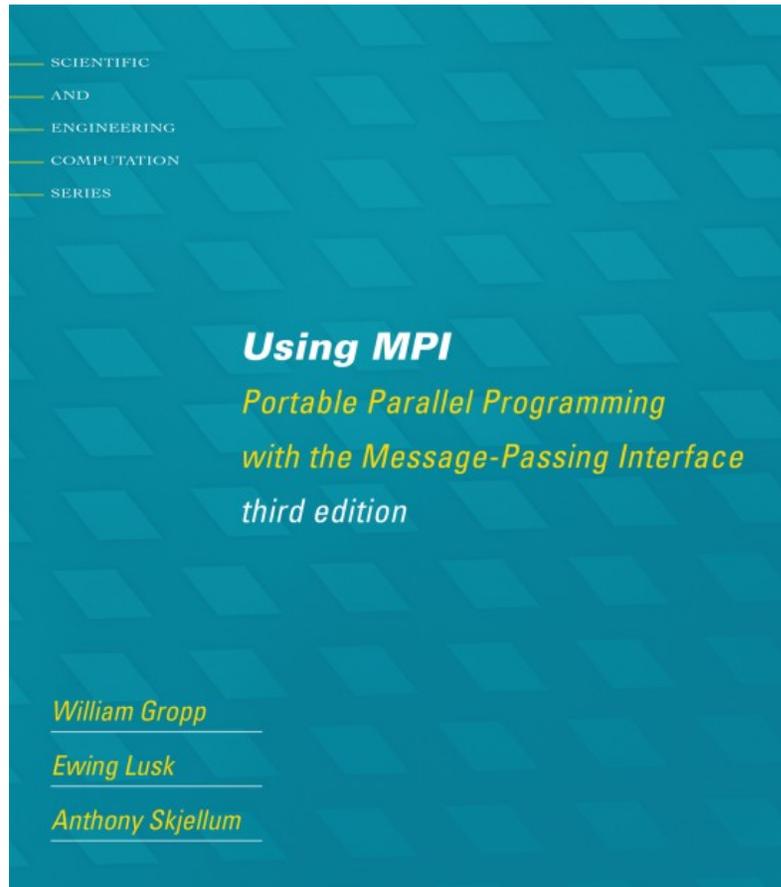
- Each MPI installation provides one or more launch scripts
  - `mpirun`
  - `mpiexec`
- On networks of workstations, launch MPI as follows
  - `mpirun [ -np PE ] [ --hostfile <filename> ] <pgm>`
    - `mpirun` will use `rsh` or `ssh` to launch jobs on machines in hostfile
    - without a hostfile, it will run all jobs on the local node
- If running under a resource manager (e.g. SLURM)
  - `srun [-n ncores] yourprogram`

# MPI Online Resources

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- <http://www.mpi-forum.org>
  - <http://www.mpi-forum.org/docs/docs.html>
    - MPI standards documents (all official releases)
- <http://www.mcs.anl.gov/research/projects/mpi/>
  - tutorials <http://www.mcs.anl.gov/research/projects/mpi/learning.html>
  - MPICH and MPICH2 implementations by ANL

# Guides to MPI Programming



# References

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- William Gropp, Ewing Lusk and Anthony Skjellum. Using MPI, 2nd Edition Portable Parallel Programming with the Message Passing Interface. MIT Press, 1999; ISBN 0-262-57132-3
- Ananth Grama, Anshul Gupta, George Karypis, and Vipin Kumar. “Introduction to Parallel Computing,” Chapter 6. Addison Wesley, 2003.
- Athas, W. C. and Seitz, C. L. 1988. Multicomputers: Message-Passing Concurrent Computers. Computer 21, 8 (Aug. 1988), 9-24. DOI= <http://dx.doi.org/10.1109/2.73>