Shared-memory Parallel Programming with Cilk Plus

John Mellor-Crummey

Department of Computer Science Rice University

johnmc@rice.edu



COMP 422/534 Lecture 4 23 January 2020

Outline for Today

- Threaded programming models
- Introduction to Cilk Plus
 - —tasks
 - -algorithmic complexity measures
 - -scheduling
 - -performance and granularity
 - -task parallelism examples
 - vector addition using divide and conquer
 - nqueens: exploratory search

What is a Thread?

• Thread: an independent flow of control

software entity that executes a sequence of instructions

- Thread requires
 - program counter
 - a set of registers
 - an area in memory, including a call stack
 - a thread id
- A process consists of one or more threads that share
 - address space
 - attributes including user id, open files, working directory, ...

An Abstract Example of Threading

A sequential program for matrix multiply

for (i = 0; i < n; i++)
for (j = 0; j < n; j++)
 c[i][j] = dot_product(get_row(a, i), get_col(b, j))</pre>



can be transformed to use multiple threads

for (i = 0; i < n; i++)
for (j = 0; j < n; j++)
c[i][col] = spawn dot_product(get_row(a, i), get_col(b, j))</pre>

Why Threads?

Well matched to multicore hardware

- Employ parallelism to compute on shared data —boost performance on a fixed memory footprint (strong scaling)
- Useful for hiding latency

 –e.g. latency due to memory, communication, I/O
- Useful for scheduling and load balancing —especially for dynamic concurrency
- Relatively easy to program —easier than message-passing? you be the judge!

Threads and Memory

- All memory is globally accessible to every thread
- Each thread's stack is treated as local to the thread
- Additional local storage can be allocated on a perthread basis
- Idealization: treat all memory as equidistant



Schema for SMP Node

Targets for Threaded Programs

Shared-memory parallel systems

- Multicore processor
- Workstations or cluster nodes with multiple processors
- Xeon Phi manycore processor —about 250 threads
- SGI UV: scalable shared memory system
 - -up to 4096 threads

Threaded Programming Models

- Library-based models
 - -all data is shared. unless otherwise specified
 - -examples: Pthreads C++11 threads, Intel Threading Building Blocks, Java Concurrency Library, Boost
- Directive-based models, e.g., OpenMP
 - -shared and private data
 - -pragma syntax simplifies thread creation and synchronization
- Programming languages
 - -Cilk Plus (Intel)
 - -CUDA (NVIDIA)
 - —Habanero-Java (Rice/Georgia Tech)

Cilk Plus Programming Model

- A simple and powerful model for writing multithreaded programs
- Extends C/C++ with three new keywords

—cilk_spawn: invoke a function (potentially) in parallel —cilk_sync: wait for a procedure's spawned functions to finish —cilk_for: execute a loop in parallel

- Cilk Plus programs specify logical parallelism
 - -what computations can be performed in parallel, i.e., tasks
 - -<u>not</u> mapping of work to threads or cores
- Faithful language extension

—if Cilk Plus keywords are elided \rightarrow C/C++ program semantics

- Availability
 - -Intel compilers

—GCC (full in versions 5 — 7; removed in version 8)

Cilk Plus Tasking Example: Fibonacci

Fibonacci sequence

0+1+1+2+3+5+8+13 21 34 55 89 144 233 377 610 987

Computing Fibonacci recursively

```
unsigned int fib(unsigned int n) {
    if (n < 2) return n;
    else {
        unsigned int n1, n2;
        n1 = fib(n-1);
        n2 = fib(n-2);
        return (n1 + n2);
    }
}</pre>
```

Cilk Plus Tasking Example: Fibonacci

Fibonacci sequence

0+1+1+2+3+5+8+13 21 34 55 89 144 233 377 610 987

Computing Fibonacci recursively in parallel with Cilk Plus

```
unsigned int fib(unsigned int n) {
  if (n < 2) return n;
  else {
    unsigned int n1, n2;
    n1 = cilk_spawn fib(n-1);
    n2 = fib(n-2);
    cilk_sync;
    return (n1 + n2);
  }
}</pre>
```

Cilk Plus Terminology

- Parallel control
 - —cilk_spawn, cilk_sync
 - -return from spawned function
- Strand

-maximal sequence of instructions not containing parallel control

```
unsigned int fib(n) {
    if (n < 2) return n;
    else {
        unsigned int n1, n2;
        n1 = cilk_spawn fib(n - 1);
        n2 = cilk_spawn fib(n - 2);
        cilk_sync;
        return (n1 + n2);
    }
}</pre>
```

Strand A: code before first spawn

Strand B: compute n-2 before 2nd spawn

Strand C: n1+ n2 before the return



Cilk Program Execution as a DAG



Cilk Program Execution as a DAG



T_P = execution time on P processors



Computation graph abstraction:

- node = arbitrary sequential computation
- edge = dependence (successor node can only execute after predecessor node has completed)
- Directed Acyclic Graph (DAG)

Processor abstraction:

- P identical processors
- each processor executes one node at a time

 T_P = execution time on P processors





 T_P = execution time on *P* processors



 $T_1 = work$ $T_{\infty} = span^*$

*Also called critical-path length

 T_P = execution time on P processors



- $T_1 = work$ $T_{\infty} = span$
- **LOWER BOUNDS** • $T_P \ge T_1/P$ • $T_P \ge T_{\infty}$

Speedup

Definition: $T_1/T_P = speedup$ on *P* processors

If $T_1/T_P = \Theta(P)$, we have *linear speedup*; = *P*, we have *perfect linear speedup*; > *P*, we have *superlinear speedup*,

Superlinear speedup is not possible in this model because of the lower bound $T_P \ge T_1/P$, but it can occur in practice (e.g., due to cache effects)

Parallelism ("Ideal Speedup")

- *T_P* depends on the <u>schedule</u> of computation graph nodes on the processors
 - two different schedules can yield different values of T_P for the same P
- For convenience, define *parallelism* (or ideal speedup) as the ratio T_1/T_{∞}
- Parallelism is independent of P, and only depends on the computation graph
- Also define *parallel slackness* as the ratio, $(T_1/T_{\infty})/P$; the larger the slackness, the less the impact of T_{∞} on performance



Example: fib(4)



Assume for simplicity that each strand in **fib()** takes unit time to execute.

Work: $T_1 = 17$ (T_P refers to execution time on P processors) *Span:* $T_{\infty} = 8$ (Span = "critical path length")

Example: fib(4)



Assume for simplicity that each strand in **fib()** takes unit time to execute.

Work: $T_1 = 17$ *Span:* $T_{\infty} = 8$ *Ideal Speedup:* $T_1/T_{\infty} = 2.125$

Using more than 2 processors makes little sense

Task Scheduling

- Popular scheduling strategies
 - -work-sharing: task scheduled to run in parallel at every spawn
 - benefit: maximizes parallelism
 - drawback: cost of setting up new tasks is high \rightarrow should be avoided
 - -work-stealing: processor looks for work when it becomes idle
 - lazy parallelism: put off setting up parallel execution until necessary
 - benefits: executes with precisely as much parallelism as needed minimizes the number of tasks that must be set up runs with same efficiency as serial program on uniprocessor
- Cilk uses work-stealing rather than work-sharing

Cilk Execution using Work Stealing

- Cilk runtime maps logical tasks to compute cores
- Approach:
 - lazy task creation plus work-stealing scheduler
 - cilk_spawn: a potentially parallel task is available
 - an idle thread steals a task from a random working thread

Possible Execution:

thread 1 begins
thread 2 steals from 1
thread 3 steals from 1
etc...











Each processor maintains a *work deque* of ready strands, and it manipulates the bottom of the deque like a stack.





Each processor maintains a *work deque* of ready strands, and it manipulates the bottom of the deque like a stack.





Each processor maintains a *work deque* of ready strands, and it manipulates the bottom of the deque like a stack.





Each processor maintains a *work deque* of ready strands, and it manipulates the bottom of the deque like a stack.





Theorem: Cilk's work-stealing scheduler achieves an expected running time of $T_P \leq T_1/P + O(T_{\infty})$ on Pprocessors

Greedy Scheduling Theorem

- Types of schedule steps
 - complete step
 - at least P operations ready to run
 - select any P and run them
 - incomplete step
 - strictly < P operation ready to run</p>
 - greedy scheduler runs them all

Theorem: On P processors, a greedy scheduler executes any computation G with work T_1 and critical path of length T_{∞} in time $T_p \leq T_1/P + T_{\infty}$

Proof sketch

- only two types of scheduler steps: complete, incomplete
- cannot be more than T_1/P complete steps, else work > T_1

— every incomplete step reduces remaining critical path length by 1 $_{-}$ no more than T_{∞} incomplete steps 34

Parallel Slackness Revisited

critical path overhead = smallest constant C_{∞} such that

$$\begin{split} T_p &\leq \frac{T_1}{P} + c_{\infty} T_{\infty} \\ T_p &\leq \left(\frac{T_1}{T_{\infty} P} + c_{\infty} \right) T_{\infty} = \left(\frac{\overline{P}}{P} + c_{\infty} \right) T_{\infty} \end{split}$$

Let $\overline{P} = T_1/T_{\infty} =$ parallelism = max speedup on ∞ processors

Parallel slackness assumption

 $\overline{P}/P >> c_{\infty}$ thus $\frac{T_1}{P} >>$

$$T_p \approx \frac{T_1}{P}$$

linear speedup

$$\frac{T_1}{P} >> c_{\infty} T_{\infty}$$

"critical path overhead has little effect on performance when sufficient parallel slackness exists" 35

Work Overhead



work overhead

$$T_p \leq c_1 \frac{T_s}{P} + c_\infty T_\infty$$

"Minimize work overhead (c_1) at the expense of a larger critical path overhead (c_{∞}) , because work overhead has a more direct impact on performance"

$$T_p \approx c_1 \frac{T_s}{P}$$

assuming parallel slackness

You can reduce C₁ by increasing the granularity of parallel work

Parallelizing Vector Addition



```
void vadd (real *A, real *B, int n) {
    int i; for (i=0; i<n; i++) A[i]+=B[i];</pre>
```

Divide and Conquer

• An effective parallelization strategy

-creates a good mix of large and small sub-problems

- Work-stealing scheduler can allocate chunks of work efficiently to the cores, as long as
 - - if work is divided into just a few large chunks, there may not be enough parallelism to keep all the cores busy
 - -not too many very small chunks
 - if the chunks are too small, then scheduling overhead may overwhelm the benefit of parallelism

Parallelizing Vector Addition

```
void vadd (real *A, real *B, int n) {
C
         int i; for (i=0; i<n; i++) A[i]+=B[i];</pre>
       void vadd (real *A, real *B, int n) {
C
         if (n<=BASE)
           int i; for (i=0; i<n; i++) A[i]+=B[i];</pre>
         } else {
           vadd (A, B, n/2);
           vadd (A+n/2, B+n/2, n-n/2);
```

Parallelization strategy:

1. Convert loops to recursion.

Parallelizing Vector Addition



Parallelization strategy:

- 1. Convert loops to recursion.
- 2. Insert Cilk Plus keywords.

Side benefit: D&C is generally good for caches!

Vector Addition





Vector Addition Analysis

To add two vectors of length *n*, where **BASE =** $\Theta(1)$:

Work: $T_1 = \Theta(n)$ Span: $T_{\infty} = \Theta(\lg n)$ Parallelism: $T_1/T_{\infty} = \Theta(n/\lg n)$



Example: N Queens

- Problem
 - —place N queens on an N x N chess board
 - -no 2 queens in same row, column, or diagonal
- Example: a solution to 8 queens problem



N Queens: Many Solutions Possible

Example: 8 queens

- 92 distinct solutions
- 12 unique solutions; others are rotations & reflections



Image credit: http://en.wikipedia.org/wiki/Eight_queens_puzzle

Sequential Recursive Enumeration of All Solutions

int nqueens(n, j, placement) {

// precondition: placed j queens so far

if (j == n) { print placement; return; }

for (k = 0; k < n; k++)

if putting j+1 queen in kth position in row j+1 is legal add queen j+1 to placement nqueens(n, j+1, placement) remove queen j+1 from placement

- Where's the potential for parallelism?
- What issues must we consider?

Parallel N Queens Solution Sketch

void nqueens(n, j, placement) {

// precondition: placed j queens so far

if (*j* == *n*) { /* *found a placement */ process placement; return;* } *for* (*k* = 1; *k* <= *n*; *k*++)

if putting j+1 queen in kth position in row j+1 is legal copy placement into newplacement and add extra queen cilk_spawn nqueens(n,j+1,newplacement)

```
cilk_sync
```

```
discard placement
```

}

Issues regarding placements

- -how can we report placements?
- -what if a single placement suffices?
 - -no need to compute all legal placements
 - —so far, no way to terminate children exploring alternate placement

Approaches to Managing Placements

- Choices for reporting multiple legal placements
 - count them
 - print them on the fly
 - collect them on the fly; print them at the end
- If only one placement desired, can skip remaining search

References

- "Introduction to Parallel Computing" by Ananth Grama, Anshul Gupta, George Karypis, and Vipin Kumar. Addison Wesley, 2003
- Charles E. Leiserson. Cilk LECTURE 1. Supercomputing Technologies Research Group. Computer Science and Artificial Intelligence Laboratory. http://bit.ly/mit-cilk-lec1
- Charles Leiserson, Bradley Kuzmaul, Michael Bender, and Hua-wen Jing. MIT 6.895 lecture notes - Theory of Parallel Systems. http://bit.ly/mit-6895-fall03
- Intel Cilk++ Programmer's Guide. Document # 322581-001US.