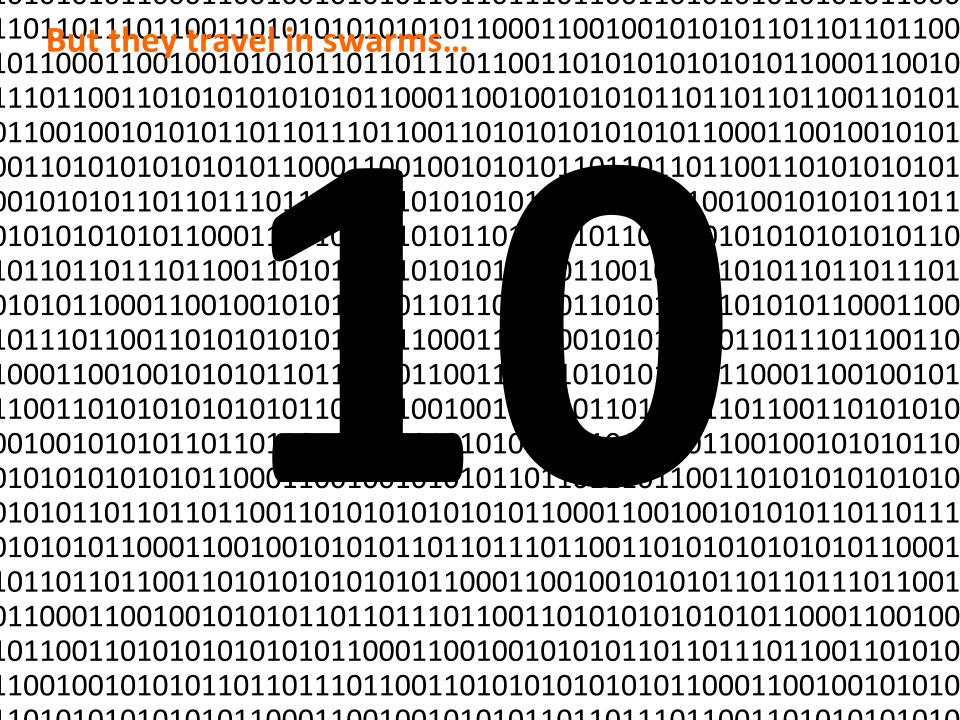


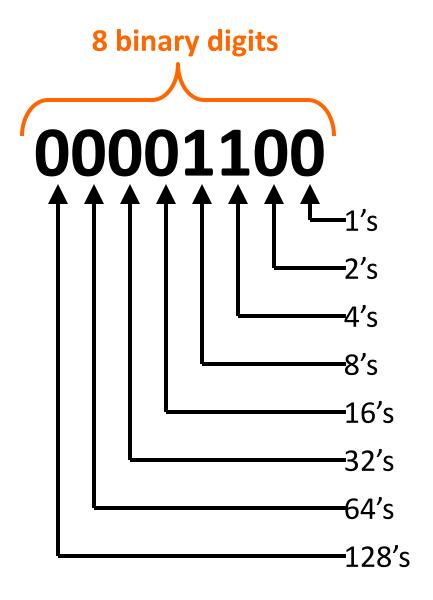
Binary Representation

The Lowly Bit

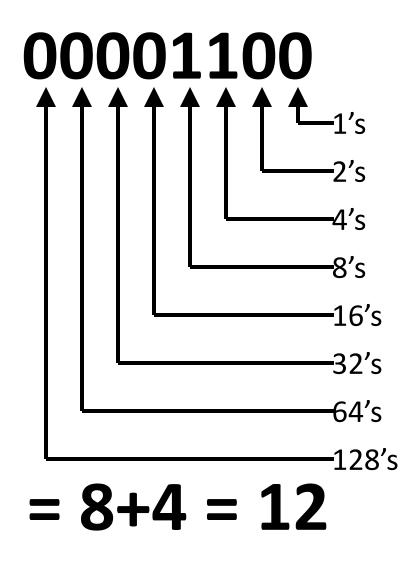




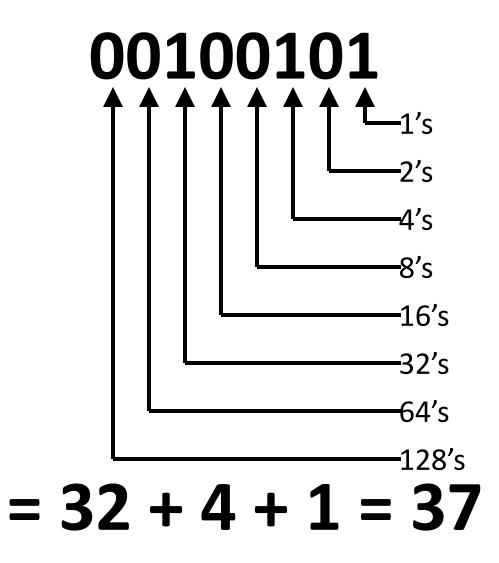
The Byte



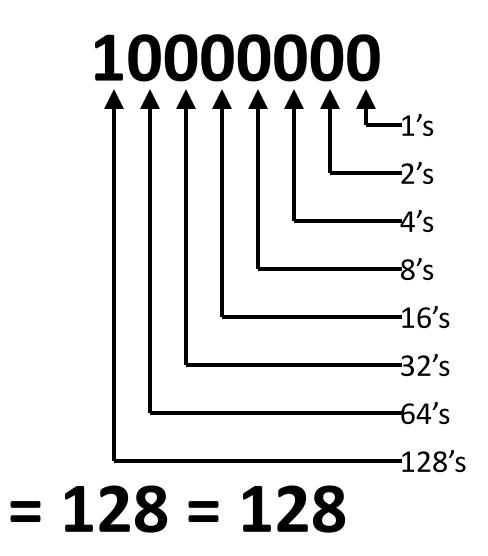
How can you read this quickly?



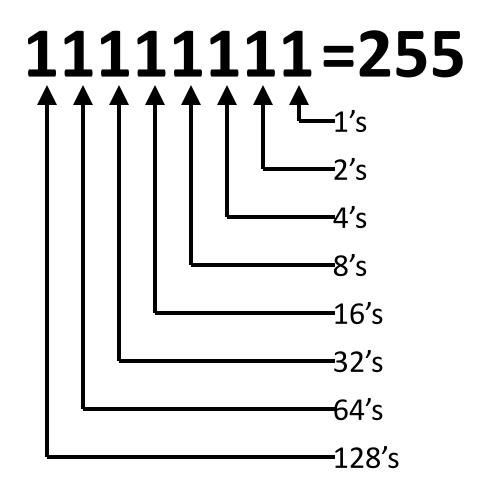
How can you read this quickly?



How can you read this quickly?



The Biggest, Baddest Byte:



Ok, so you can count, but can you add?

$$27 = 00011011$$

$$+26 = 00011010$$

ASCII Table

Easy. Assign a number to each letter.

ASCII		ASCII		ASCII		
value	Character	value	Character	value	Character	
032	(space)	064	@	096		
033	1	065	A	097	α	
034	"	066	В	098	b	
035	#	067	C	099	C	
036	\$	068	D	100	d	
037	%	069	E	101	e	
038	&	070	F	102	f	
039	<i>'</i>	071	G	103	g	
040	(072	H	104	h	
041)	073	I	105	i	
042	*	074	J	106	j	
043	+	075	K	107	k	
044	,	076	L	108	1	
045		077	M	109	m	
046	. '	078	N	110	n	
047	/	079	0	111	0	
048	0	080	P	112	p	
049	1	081	Q	113	q	
050	2	082	R	114	r	
051	3	083	S	115	S	
052	4	084	T	116	t	
053	5	085	U	117	u	
054	6	086	V	118	v	
055	7	087	W	119	w	
056	8	088	X	120	х	
057	9	089	Y	121	У	
058	:	090	Z	122	z	
059	;	091	[123	{	
060	<	092		124	1	
061	= '.	093	1	125	}	
062	>	094	^	126		
063	?	095	MANA	127		

n e

Let's write some email!

A short email: Only use 4 letters

ASCII value	Character	Control character	ASCII value	Character	ASCII value	Character	ASCII value	Character
000	(null)	NUL	032	(space)	064	@	096	
001	O	SOH	033	1	065	A	097	α
002	9	STX	034	19	066	В	098	b
003	♥	ETX	035	#	067	C	099	C
004	•	EOT	036	\$	068	D	100	d
005	*	ENQ	037	%	069	E	101	e
006	A	ACK	038	&	070	F	102	f
007	(beep)	BEL	039	t	071	G	103	g
800	10	BS	040	(072	H	104	h
009	(tab)	HT	041)	073	I	105	i
010	(line feed)	LF	042	*	074	J	106	i
011	(home)	VT	043	+	075	K	107	k
012	(form feed)	FF	044	,	076	L	108	1
013	(carriage return)	CR	045	-	077	M	109	m
014	្រា	SO	046		078	N	110	n
015	☼	SI	047	/	079	0	111	0
016		DLE	048	0	080	P	112	p
017	-400	DCl	049	1	081	Q	113	q
018	\$	DC2	050	2	082	R	114	r
019	!!	DC3	051	3	083	S	115	S
020	π	DC4	052	4	084	T	116	t
021	§	NAK	053	5	085	U	117	u
022	sisces	SYN	054	6	086	V	118	v
023	<u></u>	ETB	055	7	087	W	119	w
024	<u> </u>	CAN	056	8	088	X	120	х
025	ļ	EM	057	9	089	Y	121	У
026		SUB	058	:	090	Z	122	z
027		ESC	059	;	091	[123	{
028	(cursor right)	FS	060	<	092		124	1
029	(cursor left)	GS	061	= '	093]	125	}
030	(cursor up)	RS	062	>	094	^	126	Physical Control of the Control of t
031	(cursor down)	US	063	?	095		127	

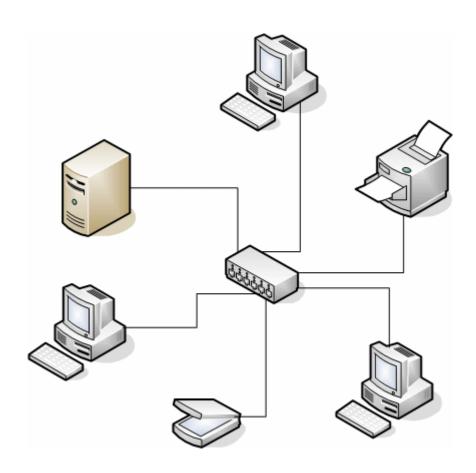
Ok, The email's done

Now how do we send it from robot to robot?



Digital Communications

We have digital communication Computers are networked



We're surrounded by Digital Communications



Ethernet



USB



3G and WiFi (This is an iPhone)



WiFi



Remote Control

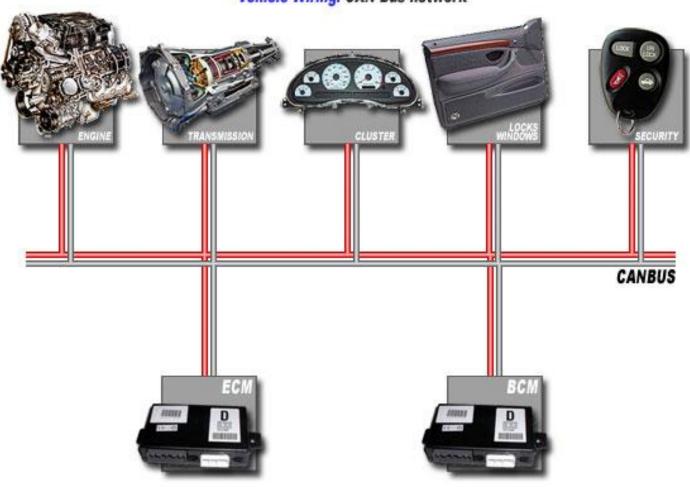


r-one robot

CAN Bus



Vehicle Wiring: CAN Bus network



Physical Representation of Digital Data



Ethernet **Voltage**



USB **Voltage**



WiFi radio waves



Remote Control IR Light



3G and WiFi radio waves



r-one robot IR Light and radio

Bandwidth

This is a measure of the amount of bits we can transmit over a channel

Its units are BPS, Bits Per Second

Anybody know some popular bandwidths?

- Ethernet = {10/100/1000} mbps
- USB 2.0 = 480 mbps
- Wi-Fi (802.11g) = 54 mbps
- r-one radio: 2 mbps, IR: 1.25 kbps

Bandwidth



Ethernet **1000 mbps**



USB 480 mbps



WiFi **54 mbps**



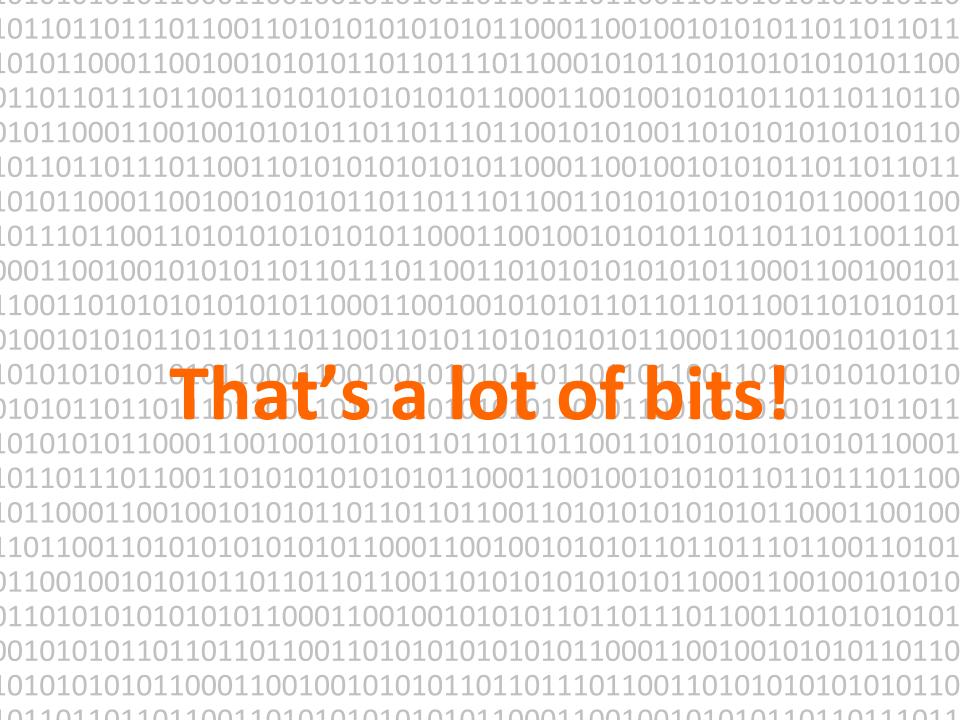
Remote Control 1.25 kbps

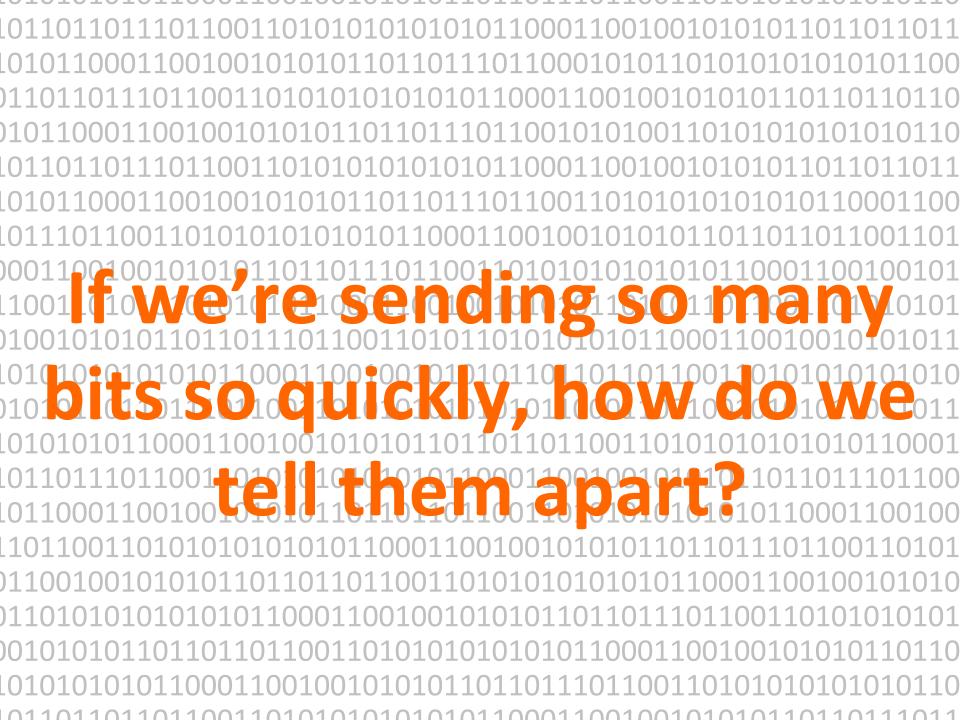


3G and WiFi
384 kbps/54 mbps



r-one robot
2 mbps/1.25 kbps





Telling one bit from another

A continuous stream of bits is hard to deal with.

Imagine a computer network: You might have many questions about these bits:

- Are these bits for you?
- Where did these bits come from?
- What do these bits mean?
- Are these bits error-free?

The Packet

A packet is a chunk of data with a well-defined beginning, end, and structure

A packet has four parts:

- Some kind of start indication that tells the network that a packet is starting
- Some kind of **header** that tells the network what the packet is, where it is from, and where it is going
- Some kind of data. That's kind of the point of the packet...
- Some kind of **error detection** to check the validity of the packet.

start header //////data///// error detection

Some easy-to-detect sequence of bits to alert the receiver that a 0110 .10011010101010101011000110010010101011011011011001101 01101110110011010101010101 101101101101100110101 01010101010110001100100101010110110110 .0010101011011011011001101010101010101100011001001

Some easy-to-detect sequence of bits to alert the receiver that a 0110 1100011001001010110110111011001101010 .100110101010101010110001100100101010110110110110011 LO1101110110011010101010101011000110010<mark>01010101</mark>L011011101100 001101010101010101100011001001010101010 0110110110110011010 10101010110001100100101010110110111 .001010101101101101100110101010101010110001100100

The Header: Routing Information

This tells the packet:

- what it is,
- where it is from, and
- where it is going

This is how everything knows where it's going

- On the internet,
- in your car,
- inside your robots,
- in between your robots via infra-red (IR),
- and in between the robots and your computer via USB

Detecting Errors

There are many sources of error in communications networks

- Errors can make our message invalid
- We highlight two: Noise and Collisions

Noise:

- Somebody comes along and changes your signal.
- They can change voltage, add radio waves, or mess with your light

Collisions:

- Somebody comes along and tries to talk at the same time
- Both messages are lost

Error Detection

Say I send you a (very) short email with your grade in ENGI 128:

'A'

(Nice job!)

In ASCII, 'A' is 65, which is 01000001 in binary

But what if an error happens during communication, and a bit is flipped? You receive:

01000011

What does this mean?

How can we prevent the bit from being flipped?

What else can we do?

Error Detection

Let's send two pieces of information: The information, and something to let us know if the data is intact

The sender composes the message data, then computes another piece of information that summarizes the message. The sender transmits:

$$check_{sender} = f(data)$$

$$msg = (data, check_{sender})$$

When the receiver gets this information, it computes its own copy of the check independently from the message data:

$$check_{receiver} = f(data)$$

If $check_{receiver} == check_{sender}$, then all is well. If not, then we discard the entire message

What can we use for *f*(data)?

Error Detection

Let's send two pieces of information: The information, and something to let us know if the data is intact

Plan A: We send the data again – the odds of getting two bits flipped in the same place are slim:

msg = 'A', which is 01000001 in binary

we send: **01000001 01000001**

For a longer message, we need lots of extra bits to detect an error:

10010101 01100101 01011001 01010110 01010101 10010101 10010101 01100101 01011001 01011001 01010110 01010101

10010101 01100101 01011001 01010110 01010101 10010101 10010101 01100101 01011001 01011001 01010110 01010101

This will take twice as much bandwidth, and bandwidth is expensive

Can we do better?

Population Count

Plan B: How about we count the total number of one bits in the message?

msg = 'A', which is 01000001 in binary

we send: **0100000100000010**

This is better. For a longer message, we still only need 8 extra bits to detect an error:

10010101 01100101 01011001 01010110 01010110 10010101 10010101 10010101 01100101 01011001 01010110 01010101 10010101

And only use one byte for Checksum. Sweet!

But there is a problem...

Checksums Behaving Badly

Plan B: How about we count the total number of bits in the message?

msg = 'A', which is 01000001 in binary

we send: **0100000100000010**

we receive: **01000010 00000010**

What is the problem?

Cyclic Redundancy Check (CRC)

Plan C: How about we make a fancy polynomial that is optimized to detect the most common errors on our communication channel?

Duh... Of course this is what we should do!

msg = 'A', which is 01000001 in binary

they send: **01000001 01101010**

we receive: **01000011 01101010**

we compute our CRC: **11101011**

They don't match. Ta-da: Error detection!

Some easy-to-detect sequence of bits to alert the receiver that a 0110 1100011001001010110110111011001101010 .100110101010101010110001100100101010110110110110011 001101010101010101100011001001010101010 0110110110110011010 10101010110001100100101010110110111 .001010101101101101100110101010101010110001100100

Some easy-to-detect sequence of bits to alert the receiver that a 0110 LO10101010101011000110010**010101**101101101100: 01010110001100100101010110110 .00101010110110110110011010101010101011000110010

r-one IR Communications

The Packet

A packet is a chunk of data with a well-defined beginning, end, and structure

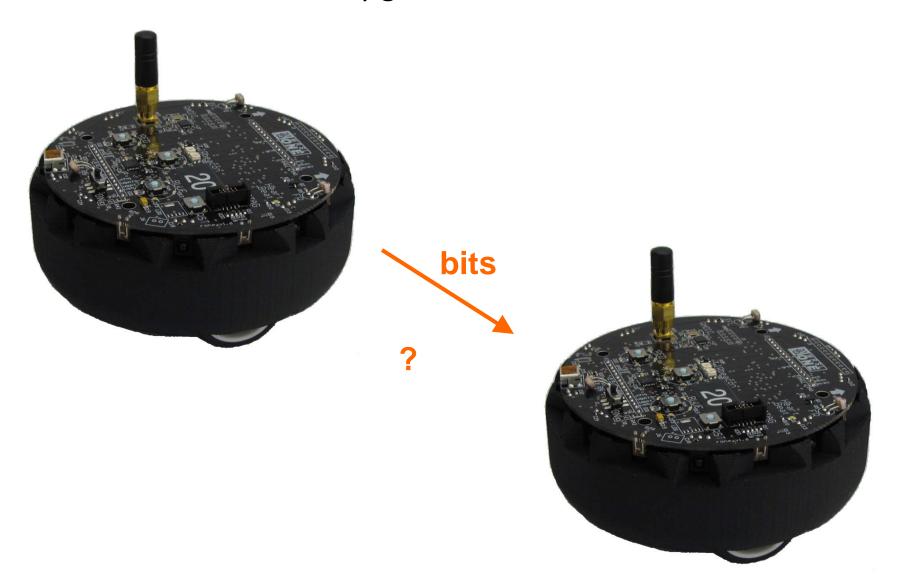
A packet has four parts:

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- Some kind of data. That's kind of the point of the packet...
- Some kind of **error detection** to check the validity of the packet.

start header //////data///// error detection

The nitty-gritty

How do these bits actually get from robot to robot?



Inter-Robot Communications

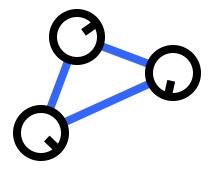
When the robots are moving, how often should they communicate?

000

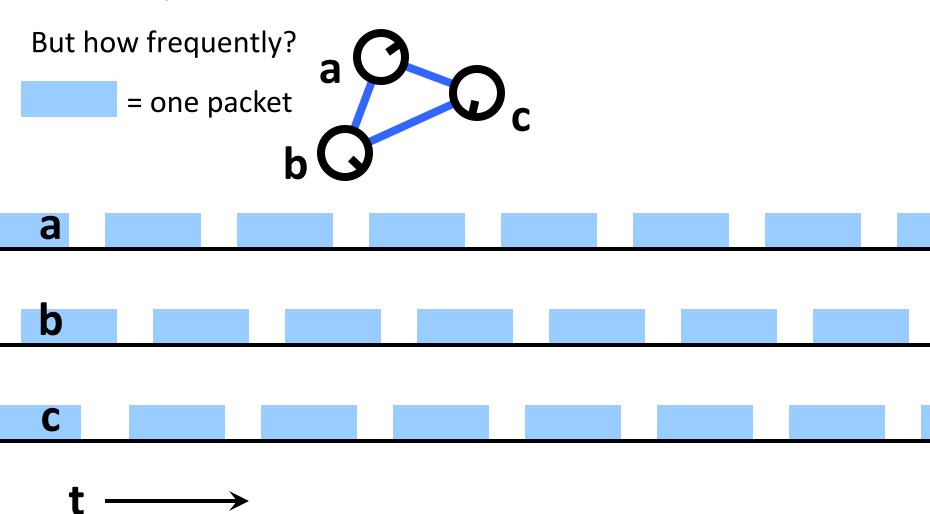
- a. all the time
- b. when they get to their goal positions
- c. only when they need to

Ok, so they need to communicate all the time

But how frequently?

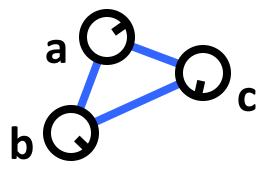


Ok, so they need to communicate all the time



We can avoid collisions with proper spacing

But now what is our problem?



a

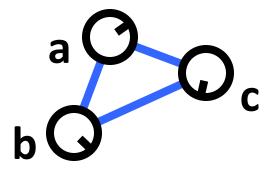
b

C

Ok, we'll be more relaxed about the timing.

But we waste ½ of the bandwidth!

Is this worth the trade-off?



a

b

C

The Neighbor "Round"

Each robot broadcasts its information to its neighbors at periodic intervals

- This period is fixed across all robots, but the starting time is random
- This gives probabilistic assurances (not guarantees) that messages won't collide (Abramson, Aloha protocol, 1970(!))

If messages are 23ms and the round is 230ms:

- 1. How many neighbors can each robot have?
- 2. What if the messages collide?
- 3. What if they all start at exactly the same time?
- 4. How does ethernet handle collisions?
- 5. Why can't we use this technique?

Measuring Local Network Geometry

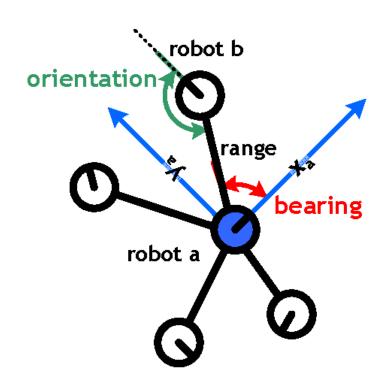
Local Coordinates

Measure pose of robot b in robot a's coordinate system

pose =
$$(x, y, \theta)$$

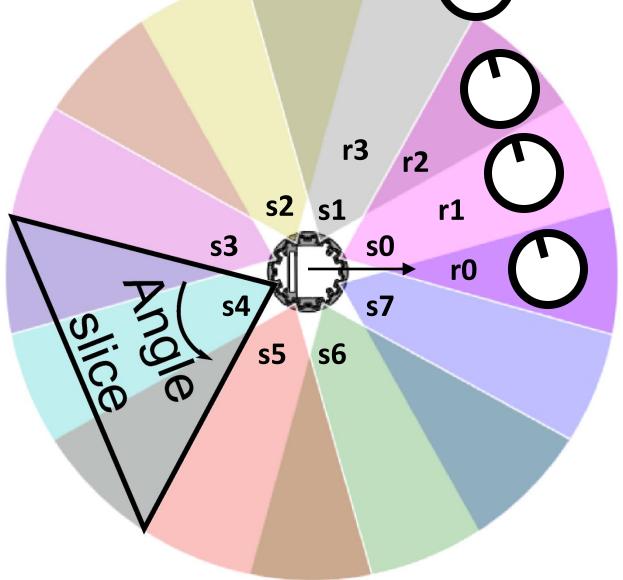
-or-

pose = (range, bearing, orientation)



IR Sectors: Bearing Measurement

8 overlapping receivers create 16 distinct re

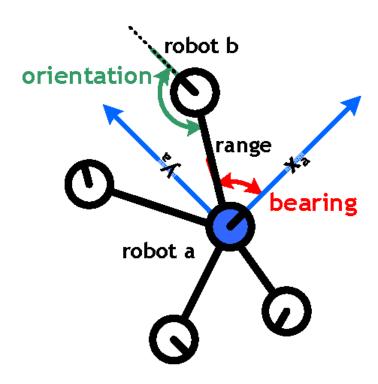


Local Coordinates: Bearing

We can measure bearing directly

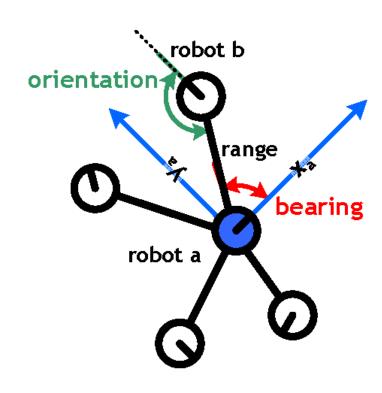
• With an accuracy of around $\pi/8$

What else can we measure?



Local Coordinates: Orientation

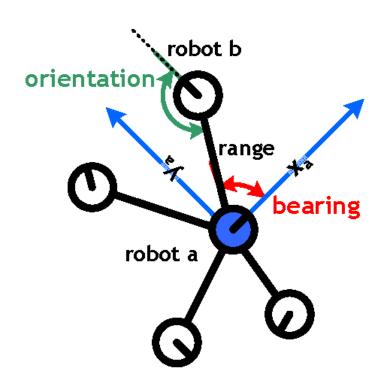
How can we measure the orientation of robot b from robot a's point of view?



Local Coordinates: Orientation

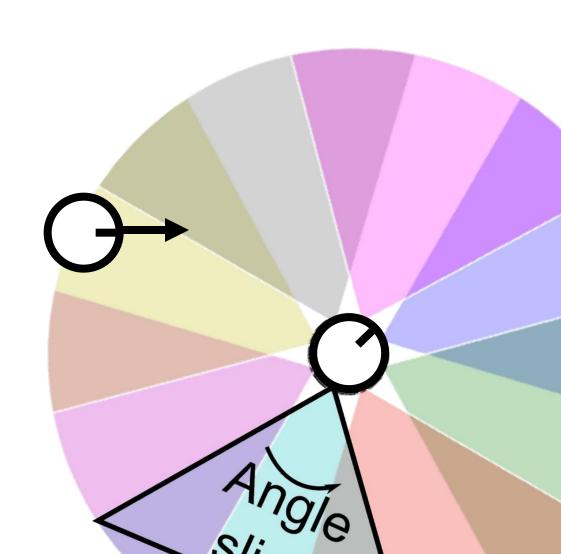
Note that the orientation of robot b from robot a's point of view is the same as the bearing of robot a from robot b's point of view

How can we get this information from robot a to robot b?



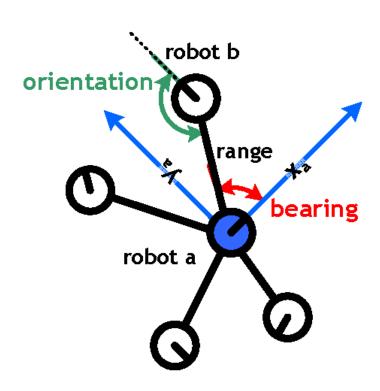
IR Sectors: Orientation Measurement

8 overlapping *transmitters* also create 16 distinct regions:



Local Coordinates: Distance

So what about distance?



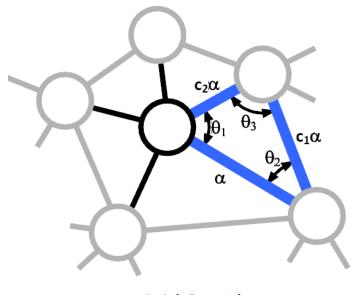
Scale-Free Coordinates

Can use angular graph rigidity to compute poses of neighbors

- Find triangles in the network
- Find the angles around this triangle
- This triangle is *rigid*: it can change size, but not shape

It's not perfect

ullet Can only compute pose up to an unknown scaling constant, lpha



a rigid 3-cycle

Particle Filters

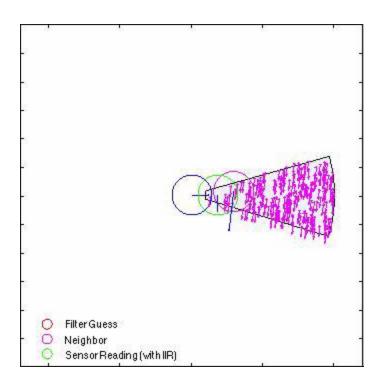
We can produce an estimate of the range over time

Local Coordinates: Improving Pose Estimates

Different sensors behave differently

- Our IR sensor resolution is limited.
- But our encoders are very precise

We can keep track of our neighbors motion to estimate where the robot is between sensor updates:



Bearing Motion Controller

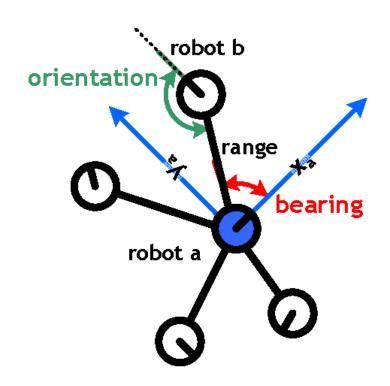
Local Coordinates

Measure pose of robot b in robot a's coordinate system

pose =
$$(x, y, \theta)$$

-or-

pose = (range, bearing, orientation)

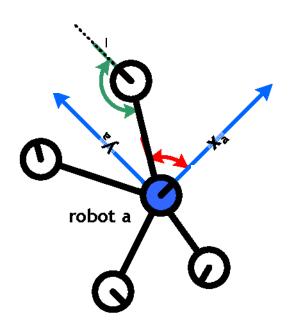


Motion Control

Instead of controlling left and right motors, it's often more convenient to control

- Translational velocity: tv, and
- Rotational velocity, rv

How can we compute left and right velocities from tv and rv?



$$v_{left} = tv - rv$$

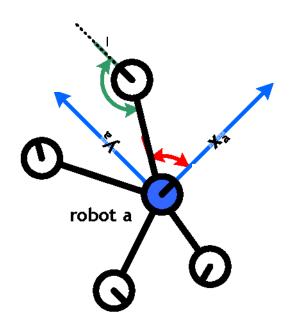
$$v_{right} = tv + rv$$

Motion Control

Instead of controlling left and right motors, it's often more convenient to control

- Translational velocity: tv, and
- Rotational velocity, rv

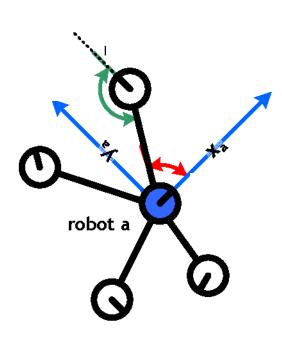
How can we compute left and right velocities from tv and rv?



$$v_{left} = tv - rv * WHEEL_BASE / 2$$

Motion Control

So, if we know the pose of a neighbor, can we compute rv and tv to get us there?



Multi-Hop Ad-hoc Networks

Communications is Necessary

This is the main difference between multi-robot systems and single robot systems

- All the data is not on a single computer
- Some kind of communications is required to cooperate

The communication cost of getting the data onto a single computer is often high

- Often too high to pay
- Multi-robot communications needs to consolidate this data somehow

OSI 7-Layer Network Stack

7. application
6. presentation
5. session
4. transport
3.network
2: data-link

1. physical

Concepts

End-to-end Principle

- Put the intelligence at the ends
- Let the stuff in the middle be stupid

Best-Effort Routing

- "We'll do out best to deliver your packet"
- No guarantee on time or path

Time

- Asynchronous: Ethernet CSMA, Exponential Random backoff
- Synchronous: Big global clock, distributed synchronizers

Routing

Flooding

- simple
- lots of wasted messages

Routing tables

- distance vector (RIP) routing
- each node has a routing table to all other nodes

Hierarchical routing

- requires much smaller routing tables
- need asymmetrical hardware to handle lots of packets
- but what if the network is changing frequently?

Graphical routing

- You can use the position of the node as a type of hierarchy
- Get packet close to the destination, then simple routing tables can do the rest

Ad-hoc networks

Sensor networks

- simple hardware
- limited bandwidth and processing

Building trees

- Use a broadcast flood
- Build efficient routing structures dynamically

r-one Summary

7. application: Shared memory API
6. presentation: n/a
5. session: n/a
4. transport: n/a
2data-link:- 24-bit-packets

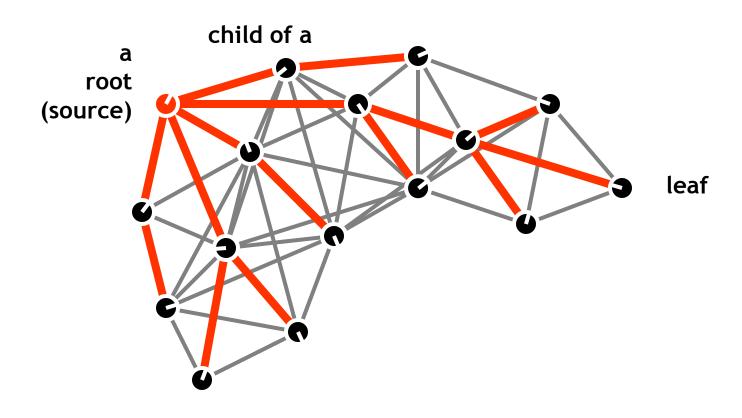
1. physical: IR with Frequency encoding

Communications in Multi-Robot Networks

Broadcast Tree Construction

Broadcast flood

Distributed BFS



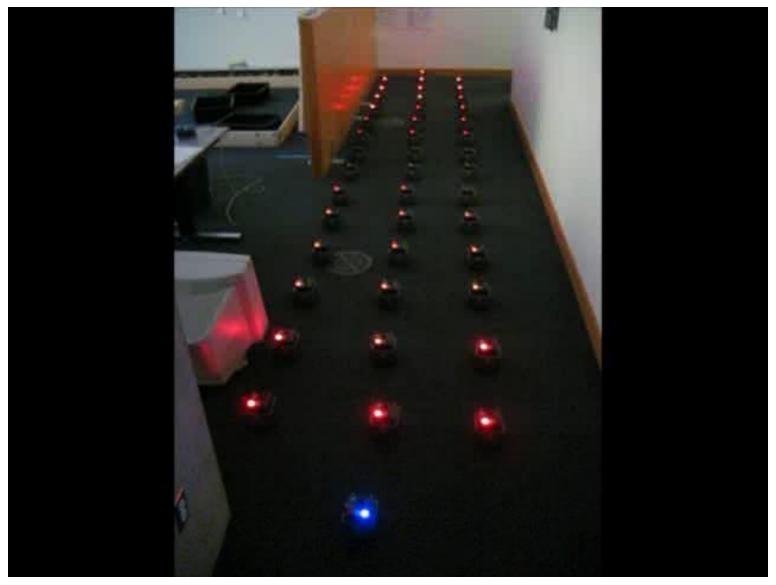
$$|E| = |V| - 1$$

[white board]

Trees, root, leaves, parents

Basic theorems

Message Speed



n = 44, $\tau = 0.250s$, speed = 0, RSR = 0

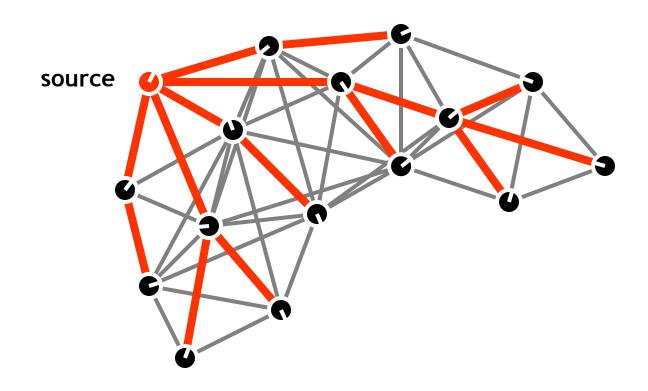
Broadcast Tree Path Distance

Purpose:

• To estimate the distance to the source of a message

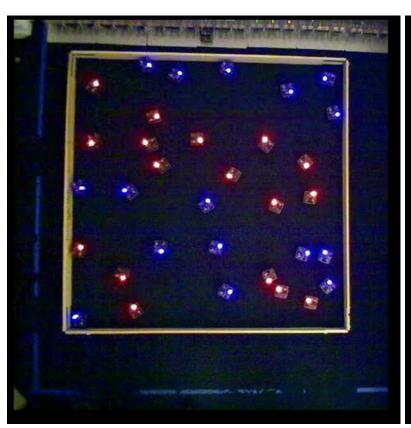
Accuracy Metric:

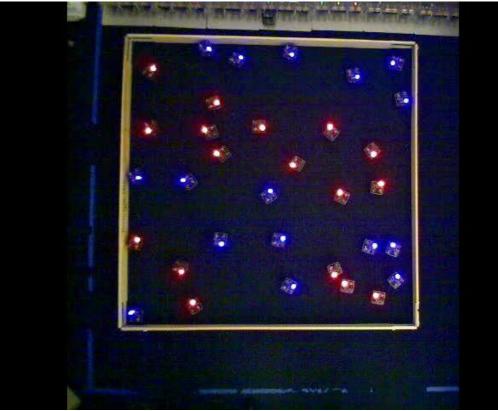
• correlation coefficient between measured and actual distances



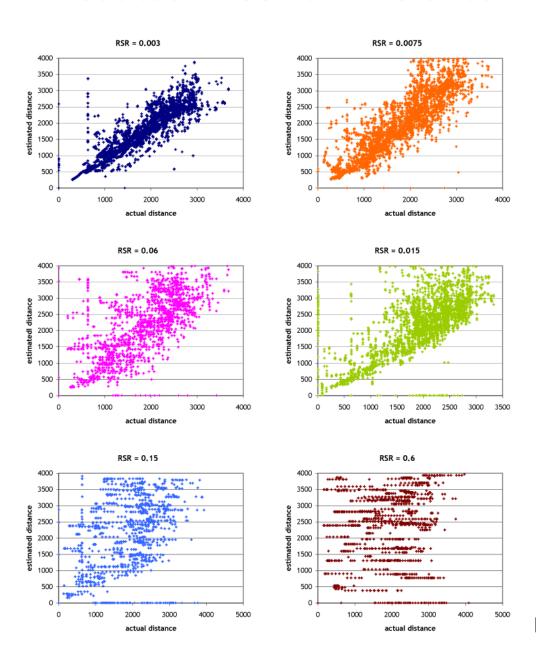
Dynamic Networks

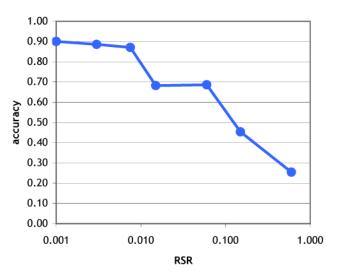
Motion "smears" network and reduces the correspondence between network topology and physical positions





Broadcast Tree Path Distance





PS02: Follow the Leader and Flocking



Follow the leader